

HEAT TRANSFER:- It is defined as "Transfer of heat from one body to another body (or) transfer of heat from one molecule to another molecule within the body."

"The transmission of energy from one region to another as a result of temperature gradient."

In heat transfer the driving potential is temperature difference whereas in mass transfer the driving potential is concentration difference. In mass transfer, we concentrate upon mass motion which result in changes in composition

Purpose/Necessity/Use of HT:-

To estimate the rate of flow of energy as heat through the boundary of a system under study

To determine the temperature field under steady and transient conditions

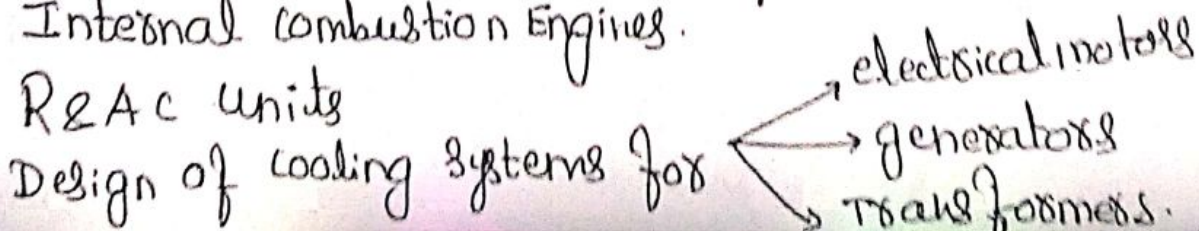
In almost every branch of engineering, HT & mass transfer problems are encountered which cannot be solved by thermodynamic reasoning alone but require an analysis based on heat transfer principles.

Areas under the discipline of HT are:-

Internal Combustion Engines.

REA units

Design of cooling systems for

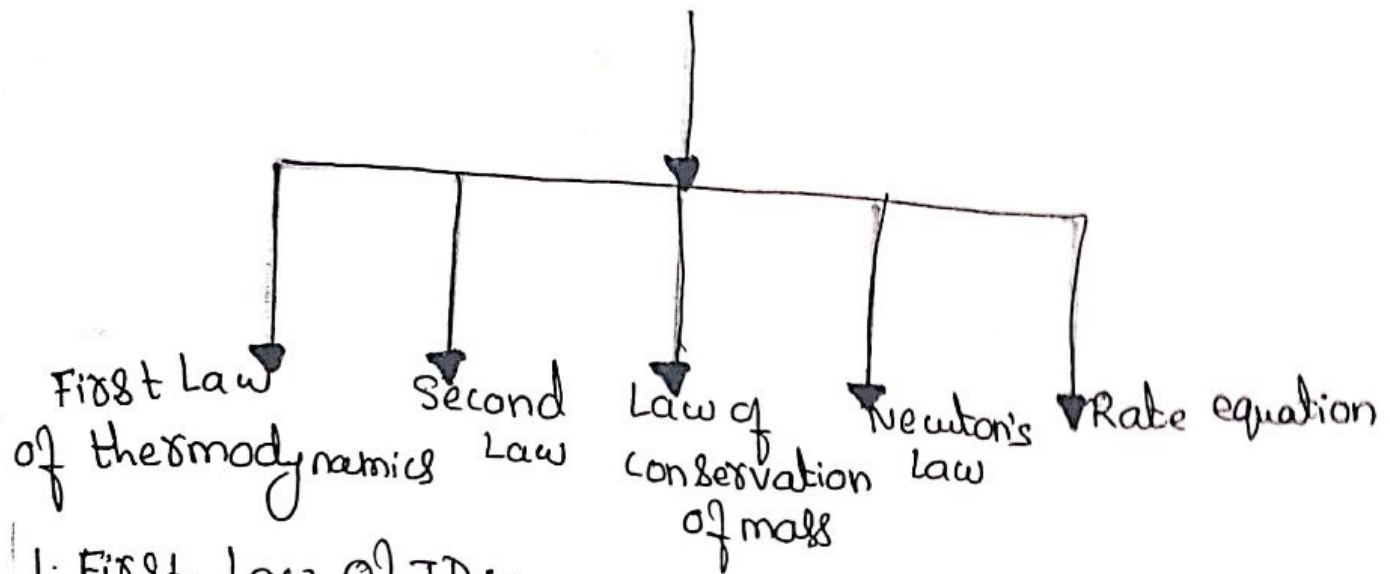


Heating and cooling of fluids.

Heat treatment of metals.

Dispersion of atmospheric pollutants

Basic Laws governing Heat Transfer



1. First Law of TD :-

$$dQ = dE + dW$$

$$dQ = du + dw$$

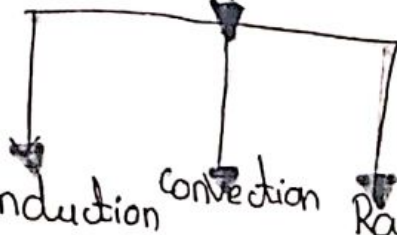
This Law can be applied to both reversible & irreversible transformations.

2. Second Law :- "Heat will naturally flow from higher reservoir to lower reservoir"

3. Law of conservation of mass :- This law is used to determine the parameter flow

4. Newton's Law :- " " " "

- modes of HT



① Conduction

It is the transfer of heat from one part of substances to another part of the same substance, or from one substance to another in physical contact with it.

Example when 2 metallic or non-metallic bodies are in contact with each other. Heat flows from high temperature region to lower temperature

Fourier's Law of heat conduction:- "The rate of flow of heat through a simple homogeneous solid is directly proportional to the area of cross-section & to the change of temperature".

Mathematically, it can be expressed as

$$Q \propto A \cdot \frac{dt}{dx}$$

$$Q = -k \cdot A \frac{dt}{dx}; \quad k = \text{Thermal conductivity}$$

where

Quantity	Represents	units
Q.	Heat flow through a body/unit time	Watts (W)
A.	surface area of heat flow	(m ²)
dt	temperature difference	°C (or) K.
dx	Thickness of body	m

Fourier Law is based on following Assumptions

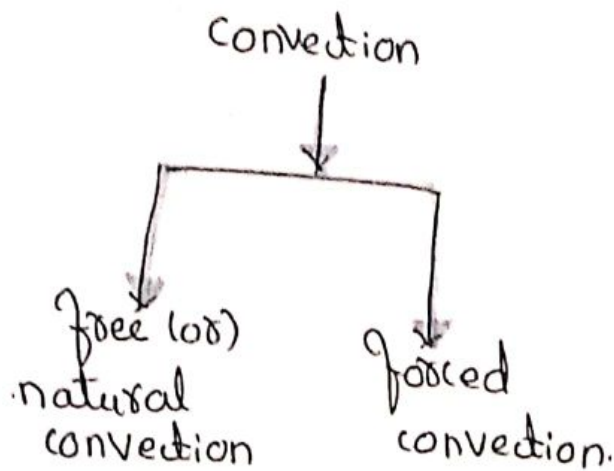
Conduction of heat takes place under steady state conditions.

- The heat flow is unidirectional.
- The temperature gradient is constant
- There is no internal heat generation.
- The material is homogeneous.

Essential Features of Fourier Law.

- It is applicable to any matter (may be liquid, solid or gas)
- It is based on experimental evidence and cannot be derived from first principle.

Heat transfer by convection :- It is defined as the transfer of heat in presence of MEDIUM.



Def of Natural Convection :- free or natural convection occurs when the fluid circulates by virtue of natural differences in densities of hot and cold fluids.

Forced Convection when the work is done to blow or pump the fluid, it is said to be forced convection

$$Q = h A (t_s - t_f) \Rightarrow h = \frac{Q}{A(t_s - t_f)} \text{ W/m}^2\text{ }^\circ\text{C}$$

Quantity	Represents	Units
Q	Rate of conductive heat transfer	Watts (W)
A	Area exposed to HT	m ²
t _s	Surface temperature	°C (or) K.
t _f	fluid temperature final "	°C (or) K.
h	Ambient " coefficient of convective heat transfer (film HT)	W/m ² °C (or) W/m ² K

Radiation:- In this mode, heat is transferred in the form of radiant energy (or) wave motion from higher temperature region to lower temperature region. It means, heat is transferred even in the absence of medium.

Examples:-

Heat is transferred from sun to earth.

Transfer of heat from thermo flask.

$$Q = F \sigma A (T_1^4 - T_2^4)$$

Quantity	Represents	Units
F	Factor depending on geometry and surface properties	
σ	Stefan-Boltzmann constant	$W m^2 K^4$
A	Area	m^2
T_1, T_2	Temperatures	$^{\circ}C$ (or) Kelvin

*

$$Q = \frac{T_1 - T_2}{[F \sigma A (T_1 + T_2) (T_1^2 + T_2^2)]}$$

[The above equation can also be written in this form]

Radiation: - In this mode, heat is transferred in the form of radiant energy (or) wave motion from higher temperature region to lower temperature region. It means, heat is transferred even in absence of medium.

Examples: -

Heat is transferred from sun to earth
Transfer of heat from thermo flask.

List some good conductors of heat and some poor conductors.

From Fourier's law of heat transfer, the rate at which heat is conducted will be proportional to the area measured normal to the direction of heat flow and to the temperature gradient in that direction.

$$Q = -KA \frac{\partial T}{\partial x}$$

$$q = \frac{-K \partial T}{\partial x} \left[\because \frac{Q}{A} = q \right]$$

The proportionality constant (K) is called coefficient of thermal conductivity.

Thermal conductivity (K) is a physical property defined as the ability of a substance to conduct heat.

Its units are $\text{W/m}^\circ\text{C}$
 W/m K .

→ Thermal conductivity for most materials can be determined experimentally by measuring the rate of heat flow and temperature gradient in the given substance.

→ The ability of conducting heat will more in substances having higher values of thermal conductivity.

Pure metals have the highest values of thermal conductivities whose " K " value decreases with increasing temperature.

Gases and vapours have the lowest thermal conductivity (K) and for them the value of K increases with increase in temperature.

Substances	K (W/mK)
Pure Silver	407.0
Pure Copper	386.0
Pure Aluminium	175.6
Mild Steel	37.2
Lead	29.8
Wood	0.15
Asbestos (fibre)	0.095
Water	0.51
Air	0.022

From table, pure metals express high value of thermal conductivity and hence are good conductors of heat.

Define the following terms.

- a) Thermal conductivity (b) Convection HT coefficient
 (c) Thermal diffusivity (d) Thermal resistance (e) Thermal conductance
 (f) Thermal contact resistance.

a) Thermal conductivity:- It is defined as the quantity of heat that passes through unit area of a plate of unit thickness in unit time when temperature difference b/w the 2 faces is maintained in degrees. It is defined by the Fourier Law

$$K = \frac{Q}{A} \frac{dx}{dt}$$

$$Q \propto \frac{K A dT}{dx}$$

$$= Q = - A K \frac{dT}{dx}$$

b) Convection HT Coefficient:- It is defined as the quantity of heat that passes through a unit area of surface in unit time for unit temperature difference b/w the fluids

write the general conduction equation for 1D heat flow with uniform heat generation unsteady state for rectangular and spherical co-ordinate systems.

Derive the general conduction equation for
 a) cylindrical coordinates
 b) Spherical co-ordinates

Heat conduction equation in rectangular co-ordinate is given by,

$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} + \frac{q}{k} = \frac{1}{\alpha} \frac{\partial T}{\partial t}$$

a) Heat Conduction Equation in cylindrical co-ordinates

Consider a small element of a cylinder whose volume is $\delta r \delta \phi \delta z$ as shown below & let it be subjected to conduction process.



Applying energy balance Equation.

$$\left[\text{Energy conducted into element / unit time} \right] + \left[\text{Internal energy / unit time} \right] = \left[\text{Increase in internal energy / unit time} \right] + \left[\text{work done by the element / unit time} \right]$$

units W/m^2K .

It mainly depends on viscosity, density, nature of flow.

Thermal diffusivity:- It is defined as the ratio of thermal conductivity to the thermal capacity. It is represented by α

$$\alpha = \frac{k}{\rho c_p}$$

Materials having higher value of α will have faster heat diffusion rate.

Thermal Resistance:- It is defined as the reciprocal of thermal conductance. It is denoted by r and mathematically represented as

$$r = \frac{\Delta x}{kA} = \frac{L}{kA}$$

It helps in making calculations on heat flow

Thermal conductance The ratio kA/L is called thermal conductance and it is the reciprocal of thermal resistance

It is represented as,

$$k_{th} = \frac{kA}{L}$$

Thermal contact Resistance. At the contact surfaces of 2 bodies the surface roughness and voids causes the contact surfaces to touch at discrete locations. This reduces the area of contact at the interface and results in resistance to flow of heat. This resistance is called as thermal conductance resistance

$$= \frac{(t_2 - t_3)}{Q/A}$$

Let Q_r be heat entering into element in radial direction, then according to Fourier's law of heat conduction

$$Q_r = -k \cdot A \frac{\partial T}{\partial r} = -k \frac{\partial T}{\partial r} r d\phi dz.$$

Let Q_{r+dr} be the heat leaving the element in radial direction at $r+dr$, then,

$$Q_{r+dr} = Q_r + \frac{\partial}{\partial r} (Q_r) \cdot dr = -k \frac{\partial T}{\partial r} r d\phi dz + \frac{\partial}{\partial r} \left[-k \frac{\partial T}{\partial r} r d\phi dz \right] dr$$

Net heat energy conducted in radial direction is

$$Q_r - Q_{r+dr} = \left[-k \frac{\partial T}{\partial r} r d\phi dz \right] - \left[-k \frac{\partial T}{\partial r} r d\phi dz + \frac{\partial}{\partial r} \left[-k \frac{\partial T}{\partial r} r d\phi dz \right] dr \right] = -k \frac{\partial}{\partial r} \left[r \frac{\partial T}{\partial r} d\phi dz dr \right] = -k \left[\frac{\partial}{\partial r} \left[r \frac{\partial T}{\partial r} \right] \cdot dr d\phi dz \right]$$

$$Q_\phi = -k \frac{\partial T}{\partial \phi} dr dz \rightarrow (1)$$

$$Q_{\phi+d\phi} = \frac{\partial}{\partial \phi} (Q_\phi) \cdot r d\phi \rightarrow (2)$$

$$(1) - (2)$$

$$Q_\phi - Q_{\phi+d\phi} = \frac{\partial}{\partial \phi} (Q_\phi) d\phi = \frac{\partial}{\partial \phi} \left[k \frac{\partial T}{\partial \phi} * dr dz \right] r d\phi = k \frac{\partial^2 T}{\partial \phi^2} r dr dz \cdot \frac{r}{\phi}$$

$$Q_z = -k \frac{\partial T}{\partial z} (r d\phi \cdot dr) \rightarrow (3)$$

$$\rightarrow (4)$$

$$Q_{z+dz} = \frac{\partial}{\partial z} (Q_z) dz = \frac{\partial}{\partial z} \left[k \frac{\partial T}{\partial z} r d\phi dz \right] = k \frac{\partial^2 T}{\partial z^2} r dr d\phi dz$$

1, 3, 7, 15, 18, 23, 31, 36, 39

(3) - (4) 40, 54

$$Q_z - Q_{z+dz} = \frac{k \partial^2 T}{\partial z^2} \times \delta \times d\delta \times d\phi \times dz$$

Net heat

$$Q_\delta - Q_{\delta+d\delta} + Q_\phi - Q_{\phi+d\phi} + Q_z - Q_{z+dz}$$

$$\Rightarrow k \left[\frac{\partial^2 T}{\partial \delta^2} + \frac{1}{\delta} \frac{\partial T}{\partial \delta} \right] \delta d\delta \cdot d\phi \cdot dz + \frac{k \partial^2 T}{\delta^2 \partial \phi^2} \delta d\delta d\phi \cdot dz + \frac{k \partial^2 T \times \delta}{\partial z^2 d\delta}$$

As there is heat conducted in element and energy generated, there will be change in Internal energy.

change in energy, $dE = \text{mass of element} \times \text{Specific heat} \times \text{change in temp}$

$$= \rho C_p \delta d\delta \cdot d\phi \cdot dz \cdot dT$$

change in IE / unit time

$$= \rho C_p \cdot \delta \cdot d\delta \cdot d\phi \cdot dz \cdot \frac{dT}{dt}$$

Substituting the values of net energy conducted in the element, element generated / unit time & change in internal energy in the energy balance equation, we get

$$k \left[\frac{\partial^2 T}{\partial \delta^2} + \frac{1}{\delta} \frac{\partial T}{\partial \delta} \right] \delta d\delta \cdot d\phi \cdot dz + \frac{k \partial^2 T}{\delta^2 \partial \phi^2} \delta \cdot d\delta \cdot d\phi \cdot dz + \frac{k \partial^2 T}{\partial z^2} \delta d\delta \cdot d\phi \cdot dz + q_0 \cdot d\delta \cdot d\phi \cdot dz = \rho C_p \delta \cdot d\delta \cdot d\phi \cdot dz \cdot \frac{dT}{dt}$$

dividing by $k \delta \cdot d\delta \cdot d\phi \cdot dz$ we get

$$\frac{\partial^2 T}{\partial x^2} + \frac{1}{r} \frac{\partial T}{\partial r} + \frac{1}{r^2} \frac{\partial^2 T}{\partial \phi^2} + \frac{\partial^2 T}{\partial z^2} + \frac{q}{k} = \frac{C \rho}{k} \frac{\partial T}{\partial t}$$

$$" " " " " = \frac{1}{2} \frac{\partial T}{\partial t}$$

Above equation in Cylindrical co-ordinates

[we can obtain this equation, from both co-ordinates in rectangular co-ordinates by substituting $x = r \cdot \cos \phi$,

$$y = r \cdot \sin \phi \text{ \& } \phi = \tan^{-1} \left[\frac{y}{x} \right] \text{ \& } z = z$$

we have,

$$\frac{\partial T}{\partial x} = \frac{\partial T}{\partial r} \cdot \frac{\partial r}{\partial x} + \frac{\partial T}{\partial y} \cdot \frac{\partial y}{\partial x}$$

$$\frac{\partial r}{\partial x} = \cos \phi \text{ \& }$$

$$\frac{\partial y}{\partial x} = \sin \phi$$

$$\text{So, } \frac{\partial T}{\partial x} = \cos \phi \frac{\partial T}{\partial r} + \sin \phi \frac{\partial T}{\partial y} \rightarrow (1)$$

$$\text{Similarly } \frac{\partial T}{\partial y} = -\sin \phi \frac{\partial T}{\partial r} + \cos \phi \frac{\partial T}{\partial y} \rightarrow (2)$$

$$\text{Equation (1)} \times \cos \phi = \cos^2 \phi \frac{\partial T}{\partial r} = \cos^2 \phi \frac{\partial T}{\partial r} + \sin \phi \cdot \cos \phi \frac{\partial T}{\partial y} \rightarrow (3)$$

$$\text{Equation (2)} \times \sin \phi = -\sin^2 \phi \frac{\partial T}{\partial r} + \sin \phi \cdot \cos \phi \frac{\partial T}{\partial y} \rightarrow (4)$$

By simplifying (3) \& (4)

$$\frac{\partial T}{\partial x} = \cos \phi \frac{\partial T}{\partial r} - \sin \phi \frac{\partial T}{\partial y}$$

$$\frac{\partial T}{\partial y} = \sin \phi \frac{\partial T}{\partial \delta} + \frac{\cos \phi}{\delta} \frac{\partial T}{\partial \phi}$$

Now, put $T = \frac{\partial T}{\partial x}$ in above equation, we get

$$\frac{\partial}{\partial x} \left(\frac{\partial T}{\partial x} \right) = \frac{\partial^2 T}{\partial x^2} = \cos \phi \frac{\partial}{\partial \delta} \left(\frac{\partial T}{\partial x} \right) - \frac{\sin \phi}{\delta} \frac{\partial}{\partial \phi} \left(\frac{\partial T}{\partial x} \right)$$

$$= \cos \phi \frac{\partial}{\partial \delta} \left[\cos \phi \frac{\partial T}{\partial \delta} - \frac{\sin \phi}{\delta} \frac{\partial T}{\partial \phi} \right] - \frac{\sin \phi}{\delta} \frac{\partial}{\partial \phi} \left[\cos \phi \frac{\partial T}{\partial \delta} - \frac{\sin \phi}{\delta} \frac{\partial T}{\partial \phi} \right]$$

∴

$$\frac{\partial^2 T}{\partial x^2} = \left[\sin^2 \phi \frac{\partial^2 T}{\partial \delta^2} + \frac{\cos^2 \phi}{\delta} \frac{\partial^2 T}{\partial \delta} - \frac{\cos \phi \cdot \sin \phi}{\delta^2} \frac{\partial T}{\partial \phi} + \frac{\cos \phi}{\delta^2} \frac{\partial^2 T}{\partial \phi^2} + \left[-\frac{\cos \phi \sin \phi}{\delta^2} \right. \right.$$

Substitute the values of $\frac{\partial^2 T}{\partial x^2}$ & $\frac{\partial^2 T}{\partial y^2}$ in heat conduction equation

heat conduction equation in rectangular co-ordinates is

$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} + \frac{q_j}{k} = \frac{1}{\alpha} \cdot \frac{\partial T}{\partial t}$$

on substituting the values of $\frac{\partial^2 T}{\partial x^2}$ & $\frac{\partial^2 T}{\partial y^2}$ we get

$$\frac{\partial^2 T}{\partial x^2} + \frac{1}{\delta} \left(\frac{\partial T}{\partial \delta} \right) + \frac{1}{\delta^2} \cdot \frac{\partial^2 T}{\partial \phi^2} + \frac{\partial^2 T}{\partial z^2} + \frac{q_j}{k} = \frac{1}{\alpha} \cdot \frac{\partial T}{\partial t}$$

†††

39

23

15

38

①
What is transient heat conduction? How does this differ from steady conduction?

A body in which there is no change in its temperature const. time, such a body is said to be in a Steady state.

If there is no change in the surface temperature of the body, it attains an equilibrium temp, after some period called the Steady state.

If the temp. of the body varies with some time period then the body is said to be in unsteady state. This unsteady state is also called as transient state.

The transient condition take place in the following system.

- ①. cooling of IC engines
- ②. cooling & freezing of food
- ③. Vulcanization of rubbers
- ④. For making bricks.

Lumped capacity & Assumptions:-

It is a type of analysis which reduces a thermal system to number of discrete lumps and assume that the difference in temp. inside each lump is negligible.

It is applicable to transient heat flow conduction problems.

Assumptions:-

- ①. Internal conductive resistance of the system is very small.
- ②. The temp. within the system at any instant is uniform
- ③. It assumes temp. inside a solid is constant
- ④. It deals with heat transfer b/w solid & ~~and~~ ambient fluids.

①. A chrome-nickel wire of 2mm diameter initially at 25°C , is suddenly exposed to hot gases at 725°C . If the convection HT coefficient is $10 \text{ W/m}^2\text{-K}$. Calculate the time constant of the wire as lumped capacity system. Take $k = 20 \text{ W/m-K}$, $\rho = 7800 \text{ kg/m}^3$, $C_p = 0.46 \text{ kJ/kg-K}$.

Sol Given data.

$$D = 2 \text{ mm} = 2 \times 10^{-3} \text{ m}$$

$$t_{\infty} = 25^{\circ}\text{C}$$

$$t_i = 725^{\circ}\text{C}$$

$$h = 10 \text{ W/m}^2\text{-K}$$

$$k = 20 \text{ W/m-K}$$

$$\rho = 7800 \text{ kg/m}^3$$

Lumped capacity system is applicable to the cases with Biot No < 0.1

$$\therefore \boxed{Bi = \frac{hL_c}{k}}$$

here L_c is unknown. finding L_c .

$$L_c = \frac{D}{4} \text{ (for cylindrical shapes)}$$

$$L_c = \frac{2 \times 10^{-3}}{4}$$

$$Bi = \frac{h L_c}{k} \Rightarrow \frac{10 \times 2 \times 10^{-3}}{20 \times 4}$$

$$Bi = 2.5 \times 10^{-4} < 0.1$$

$$\therefore \text{Time constant} = \frac{\rho C_p V}{h A_s} = \frac{k V}{\alpha h A_s}$$

where,

$$\rho = \text{density} = 7800 \text{ kg/m}^3$$

$$C_p = \text{Specific heat} = 0.46 \text{ kJ/kg-K}$$

$$V = \text{Volume of cylinder} = \frac{\pi}{4} D^2 L$$

$$A_s = \text{Surface area of cylinder} = \pi D L$$

$$\alpha = \text{Thermal diffusivity in m}^2/\text{sec}$$

$$= \frac{7800 \times 0.46 \times 10^3}{10} \times \frac{\frac{\pi}{4} D^2 L}{\pi D L}$$

$$= \frac{7800 \times 0.46 \times 10^3}{10} \times \frac{2 \times 10^{-3}}{4}$$

$$= 179.4 \text{ seconds}$$

2. A cylindrical nickel steel billet of 0.1 m diameter & 0.5 m length, initially at 800°C is suddenly dropped in a large vessel containing oil at 30°C .

The convective heat transfer coefficient b/w the billet and the oil is $20 \text{ W/m}^2\text{K}$. Calculate the time required for the billet to reach a temperature of 250°C . Take for nickel, steel, $k = 20 \text{ W/m}\cdot\text{K}$, $\rho = 8000 \text{ kg/m}^3$, $c_p = 0.45 \text{ kJ/kg}\cdot\text{K}$.

Sol Given data

$$L = 0.5 \text{ m}$$

$$D = 0.1 \text{ m}$$

$$T_0 = 800^{\circ}\text{C}$$

$$T_{\infty} = 30^{\circ}\text{C}$$

$$h = 20 \text{ W/m}^2\text{K}$$

$$k = 20 \text{ W/m}\cdot\text{K}$$

$$\rho = 8000 \text{ kg/m}^3$$

$$c_p = 0.45 \text{ kJ/kg}\cdot\text{K}$$

$$= 450 \text{ J/kg}\cdot\text{K}$$

$$\text{Biot No} = \frac{hL_c}{k}$$

$$L_c = \frac{V}{A} = \frac{D}{4}$$

$$L_c = \frac{0.1}{4} = 0.025$$

$$\left[\begin{array}{l} \bullet \bullet V = \frac{\pi}{4} D^2 L = \frac{\pi}{4} (0.1)^2 \times 0.5 = 3.927 \times 10^{-3} \\ \bullet A = \pi D L = \pi \times 0.1 \times 0.5 = 0.157 \text{ m}^2 \end{array} \right.$$

$$\text{Bi} = \frac{hL_c}{k}$$

$$= \frac{20 \times 0.025}{20} = 0.025 < 0.1$$

$\therefore \text{Bi} < 0.1$, Lumped capacity analysis applicable

$$\frac{T - T_\infty}{T_0 - T_\infty} = e^{\left[\frac{-hA}{\rho c V} \right] \times t}$$

$$\Rightarrow \frac{250 - 30}{800 - 30} = e^{- \left[\frac{20 \times 0.157}{8000 \times 450 \times 3.927 \times 10^{-3}} \right] t}$$

$$\Rightarrow 0.2857 = e^{-222.1 \times 10^{-6} t}$$

$$-1.2528 = -222.1 \times 10^{-6} t$$

$$t = \frac{1.2528}{222.1 \times 10^{-6}} = 5640.7 \text{ seconds}$$

$$\Rightarrow t = \frac{5640.7}{60 \times 60} = \underline{1.567 \text{ hours}}$$

③. A solid copper cylinder of 5cm diameter was dropped into ice water after recording the temp as 20°C . After 3 minutes, the temp. of cylinder is again measured & recorded as 1°C . Calculate the convective HT coefficient by taking ρ & C_p of copper 8600 kg/m^3 & 334.945 J/kg-K . Neglect the thermal resistance of the cylinder.

Sol given data.

$$\text{Time, } \tau = 3 \text{ minutes} = 180 \text{ sec.}$$

$$d = 5 \text{ cm} = 0.05 \text{ m}$$

$$T_i = 20^{\circ}\text{C}$$

$$T = 1^{\circ}\text{C}$$

$$T_{\infty} = 0^{\circ}\text{C} \text{ (}\because \text{ fluid is ice water)}$$

$$\rho = 8600 \text{ kg/m}^3$$

$$C = 334.945 \text{ J/kg-K.}$$

$$\text{Formula} \rightarrow \frac{T - T_{\infty}}{T_i - T_{\infty}} = e^{\left[\frac{-hAs}{\rho V C} \times \tau \right]}$$

$$V = \frac{\pi}{4} d^2 L$$

$$As = \pi d L$$

$$\left[\frac{1-0}{20-0} \right] = e^{\left[\frac{-h \cdot 80(180)}{334.94 \times 8600} \right]}$$

$$0.05 = e^{[-4.999 \times 10^{-3} h]}$$

$$\ln(0.05) = -4.999 \times 10^{-3} h$$

$$\Rightarrow -2.9957 = -4.999 \times 10^{-3} h$$

$$h = \frac{-2.9957}{4.999 \times 10^{-3}}$$

$$h = 599.26 \text{ W/m}^2\text{K}$$

④. An aluminium sphere of 0.1m diameter and at a uniform temperature of 500°C, with $h = 30 \text{ W/m}^2\text{K}$. Calculate the temp of sphere.

a) 100 s

b) 300 s

c) 500 s after it is exposed to the environment

Justify any method you use for the analysis.

Take, for aluminium

$k = 200 \text{ W/mK}$, $\rho = 2700 \text{ kg/m}^3$, $c_p = 0.9 \text{ kJ/kg} \cdot \text{K}$

Sol Given data.

$$D = 0.1 \text{ m.}$$

$$R = 0.05 \text{ m.}$$

$$T_1 = 500^\circ\text{C}$$

$$T_\infty = 20^\circ\text{C}$$

$$h = 30 \text{ W/m}^2\text{-K.}$$

$$k = 200 \text{ W/m-K.}$$

$$\rho = 2700 \text{ kg/m}^3$$

$$c_p = 0.19 \text{ kJ/kg-K, } c_p = 900 \text{ J/kg-K.}$$

$$Bi = \frac{hL_c}{k} = \frac{30 \times 0.0166}{200}$$
$$= 2.5 \times 10^{-3} = 0.0025$$

$$\underline{Bi} < 0.1$$

hence lumped heat analysis is applied

$$a) \frac{T_2 - T_\infty}{T_1 - T_\infty} = \exp\left[\frac{hA\tau}{\rho c_p V}\right]$$

$$\frac{T_2 - 20}{500 - 20} = \exp\left[-\left[\frac{h}{\rho c_p}\right] \times \left(\frac{A}{V}\right) \times \tau\right]$$

$$\text{Let } \left[\frac{h}{\rho c_p}\right] \times \left(\frac{A}{V}\right) = X.$$

$$\alpha = \left[\frac{30}{2700 \times 900} \right] \left[\frac{1}{0.0166} \right]$$

$$\left[\because \frac{V}{A} = 0.0166 \right]$$

$$\alpha = 7.4059 \times 10^{-4}$$

Substituting α in formula.

$$\frac{T_2 - 20}{480} = \exp^{-(7.4059 \times 10^{-4}) \times 100}$$

$$T_2 - 20 = 480 \times 0.9283$$

$$T_2 = 20 + 445.584$$

$$\boxed{T_2 = 465.584^\circ\text{C}}$$

$$b) \frac{T_3 - 20}{480} = e^{-(\alpha t)}$$

$$\frac{T_3 - 20}{480} = e^{-(7.4059 \times 10^{-4}) \times 300}$$

$$T_3 - 20 = 480 \times 0.80077$$

$$T_3 = 20 + 384.37$$

$$\boxed{T_3 = 404.37^\circ\text{C}}$$

$$c) \frac{T_4 - 20}{480} = e^{-(\alpha t)}$$

$$T_4 - 20 = 480 \times e^{-(7.4059 \times 10^{-4}) \times 500}$$

$$T_4 - 20 = 331.45$$

$$T_4 = 331.45 + 20$$

$$T_4 = 351.45^\circ\text{C}$$

5. A large slab of aluminium has a thickness of 10 cm is initially uniform at temp of 400°C . Suddenly exposed to a convection environment at 90°C with $h = 1400 \text{ W/m}^2\text{-K}$. How long does it take the center line temp to drop to 180°C ?

Sol Thickness, $L = 10 \text{ cm}$.

$$T_i = 400^\circ\text{C}$$

$$T_\infty = 90^\circ\text{C}$$

$$h = 1400 \text{ W/m}^2\text{-K}$$

$$T = 180^\circ\text{C}$$

$$k = 206 \text{ W/m-K (assuming)}$$

$$\alpha = 84.18 \times 10^{-6} \text{ m}^2/\text{s (")}$$

$$Bi = \frac{hL_c}{k}$$

$$L_c = \frac{L}{2} = \frac{10}{2} = 5 \text{ cm} = 0.05 \text{ m}$$

$$Bi = \frac{1400 \times 0.05}{200} = 0.3398$$

∵ $Bi > 0.1$ & less than 100

$Bi > 0.1$
 $Bi < 100$ } ∴ we can use Heisler charts.

$$\frac{T - T_\infty}{T_i - T_\infty} = \frac{180 - 90}{400 - 90} = 0.2903$$

From Heisler charts, corresponding to $Bi = 0.3398$

Fouriers No, $F_0 = 4.2$.

$$F_0 = \frac{\alpha T}{L_c^2}$$

⇒ finding γ

$$4.2 = \frac{84.18 \times 10^{-6} \times \gamma}{(0.05)^2}$$

$$\gamma = \frac{4.2 \times (0.05)^2}{84.18 \times 10^{-6}}$$

$$= 124.73 \text{ seconds}$$

$$T = \frac{Q \cdot \lambda}{k \cdot t}$$

$$= \frac{Q \cdot \lambda}{k \cdot t}$$

Q. on a hot summer's day concrete highway reach to temperature of 55°C . Suppose that a stream of H_2O is directed on the highway so that the surface temp is suddenly lowered to 35°C . How long it will take to cool the concrete to 45°C at a depth of 5cm from the surface?

Sol Given Data:

$$T_i = 55^{\circ}\text{C}$$

$$T_{\infty} = 35^{\circ}\text{C}$$

$$t = ?$$

$$T_0 = 45^{\circ}\text{C}$$

$$\lambda = 5\text{cm} = 0.05\text{m}$$

$$\frac{T - T_{\infty}}{T_i - T_{\infty}} = \text{erf} \left[\frac{\lambda}{2\sqrt{\alpha t}} \right]$$

$$\frac{45 - 35}{55 - 35} = \text{erf} \left[\frac{0.05}{2\sqrt{\alpha t}} \right]$$

$$0.5 = \text{erf} \left[\frac{0.05}{2\sqrt{\alpha t}} \right]$$

Different Types of flows in convective HT:-

I. Causation of flow.

a) mixed & unmixed flow.

b) Natural & forced flow.

II. Condition of flow

a) steady & unsteady flow.

b) compressed, & incompressible flow.

c) laminar & Turbulent flow.

III configuration of flow.

a) I, II & IV D flows.

b) Internal & external flows.

IV Medium of flow.

a) viscous flow.

Eg:- oil, water

b) Inviscid flow.

Eg:- Gases.

LAMINAR FLOW

1. Flow follows a smooth continuous path
2. No transverse movement of fluid particles
3. $Re < 2000$ describes a laminar flow
4. Head loss \propto Velocity
 $\propto h_f \propto V$
5. Flow of high viscosity fluid at low velocity has laminar flow
Example: oil

TURBULENT FLOW

1. Flow follows a random (or) irregular path.
2. Transverse displacement of fluid particles
3. $Re > 4000$ describes a turbulent flow.
4. Head loss \propto nth power of velocity
 $h_f \propto V^n$.
5. Flow of low viscosity fluids at high velocity has turbulent flow
Example: Air

Q. Air at 27°C flows over a flat plate at a velocity of 2 m/s . The plate is heated over its entire length to a temp of 60°C . Calculate the HT for the first 20 cm of the plate.

Sol Given data.

$$T_{\infty} = 27^{\circ}\text{C}$$

$$U = 2\text{ m/s}$$

$$T_s = 60^{\circ}\text{C}$$

$$x = 20\text{ cm} = 0.2\text{ m}$$

$$T_f = \frac{27 + 60}{2} = \frac{87}{2} = 43.5^{\circ}\text{C}$$

Physical properties of air at 43.5°C .

$$\nu = 17.3 \times 10^{-6} \text{ m}^2/\text{s}$$

$$k = 0.0278$$

$$P_r = 0.679$$

$$Re = \frac{Ux}{\nu}$$

$$= \frac{2 \times 0.2}{17.3 \times 10^{-6}} = 2.31 \times 10^4$$

$$Nu = 0.332 \times Re^{1/2} \times P_r^{1/3}$$

$$= 0.332 \times (2.31 \times 10^4)^{1/2} \times (0.679)^{1/3}$$

$$Nu = 44.35$$

$$Nu = \frac{hL}{k}$$

$$44.35 = \frac{h \times 0.2}{0.0278}$$

$$h = \frac{44.35 \times 0.0278}{0.2}$$

$$h = 6.16 \text{ W/m}^2\text{K}$$

$$\begin{aligned} \text{Avg. HT coefficient, } \bar{h} &= 2 \times 6.16 \\ &= 12.32 \text{ W/m}^2\text{K} \end{aligned}$$

$$Q = \bar{h}A (T_s - T_\infty)$$

$$\begin{aligned} \frac{Q}{A} = q &= 12.32 (60 - 27) \\ &= 406.56 \text{ W/m}^2 \end{aligned}$$

②. Air at 20°C & 1 atmosphere flows over a flat plate at 35 m/s . The plate is 75 cm long & is maintained at 60°C . Calculate the HT from the plate/unit width of plate. Also calculate the turbulent boundary layer thickness at the end of the plate assuming it to develop from the leading edge of plate.

Sol given data.

$$T_d = 20^\circ\text{C}$$

$$T_s = 60^\circ\text{C}$$

$$u = 35 \text{ m/s}$$

$$L = 75 \text{ cm} = 0.75 \text{ m}$$

$$T_f = \frac{20 + 60}{2} = \frac{80}{2} = 40^\circ\text{C}$$

The properties of air at 40°C ,

$$\nu = 16.96 \times 10^{-6} \text{ m}^2/\text{s}$$

$$k = 0.02756 \text{ W/mK}$$

$$P_r = 0.669$$

$$Re = \frac{uL}{\nu} = \frac{35 \times 0.75}{16.96 \times 10^{-6}} = 1547759.43$$

From tables, mean value of Nu is

$$\begin{aligned} Nu &= \frac{hL}{k} = P_r^{1/3} (0.037 \times Re^{0.8} - 871) \\ &= (0.669)^{1/3} [0.037 \times (1547759.43)^{0.8} - 871] \\ &= 2134.056 \end{aligned}$$

$$h_L = \frac{NU \times k}{L}$$

$$= \frac{2134.056 \times 0.02756}{0.75}$$

$$= 78.419 \text{ W/m}^2\text{k.}$$

$$Q = hA\Delta t$$

$$= 2 \times 78.419 \times 0.75 (60 - 20)$$

$$= 4705.140 \text{ W}$$

$$\phi \delta_{hx} = 0.37 \times L \times Re^{-0.2}$$

$$= 0.37 \times 0.75 (1547759.43)^{-0.2}$$

$$= 0.016 \text{ m}$$

$$= 16 \text{ mm}$$

③ Water at 20°C was flowing over a plate of uniform heat flux of 9000 W/m². The flow velocity was 200 mm/s. The length of the plate was 1.3 m.

Determine the temp of the plate.

Say Given data.

$$T_d = 20^\circ\text{C.}$$

$$q = 9000 \text{ W/m}^2$$

$$u = 200 \text{ mm/s}$$

$$= 0.2 \text{ m/s}$$

$$L = 1.3 \text{ m}$$

Properties of water at 20°C are,

$$\nu = 1.006 \times 10^{-6} \text{ m}^2/\text{s}$$

$$Pr = 7.020$$

$$k = 0.5978 \text{ W/mK}$$

$$Re = \frac{uL}{\nu}$$

$$= \frac{0.2 \times 1.3}{1.006 \times 10^{-6}}$$

$$= 2.58 \times 10^5$$

$$= 2.58 \times 10^5 < 5 \times 10^5$$

$$Nu = 0.662 \cdot Re^{1/2} \cdot Pr^{1/3}$$

$$= 0.662 \cdot (2.58 \times 10^5)^{1/2} \cdot (7.020)^{1/3}$$

$$= 643.84$$

$$Nu = \frac{hL}{k}$$

$$643.84 = \frac{hL}{k}$$

$$643.84 = \frac{h \cdot 1.3}{0.5978}$$

$$h = \frac{643.84 \times 0.5978}{1.3}$$

$$h = 295.88 \text{ W/m}^2\text{K}$$

$$Q = hA\Delta t \Rightarrow \frac{Q}{A} = h\Delta t \Rightarrow q_v = h\Delta t$$

$$q = h(T_s - T_\infty)$$

$$9000 = 295.88(T_s - 20)$$

$$T_s = 50.41^\circ\text{C}$$

④ Air at 35°C flows across a cylinder of 50 mm diam at a velocity of 50 m/s. The cylinder surface is maintained at 145°C . Calculate the heat loss/length of the cylinder.

Sol Given Data.

$$T_s = 145^\circ\text{C}$$

$$T_\infty = 35^\circ\text{C}$$

$$V = 50 \text{ m/s}$$

$$d = 50 \text{ mm} = 0.05 \text{ m}$$

$$T_f = \frac{145 + 35}{2} = 90^\circ\text{C}$$

At $T_f = 90^\circ\text{C}$, properties of air are,

$$\mu = 21.48 \times 10^{-6} \text{ N s/m}^2$$

$$k = 0.03128 \text{ W/mK}$$

$$c_p = 1009 \text{ J/kgK}$$

$$\rho = 0.972 \text{ kg/m}^3$$

$$Re = \frac{Lvd}{\mu}$$

$$= \frac{0.972 \times 50 \times 0.05}{21.48 \times 10^{-6}}$$

$$= 0.113 \times 10^6 = 1.13 \times 10^5$$

$$Pr = \frac{\mu C_p}{k}$$

$$= \frac{21.48 \times 10^{-6} \times 1009}{0.03128}$$

$$= 0.692$$

$$Nu = 0.027 Re^{0.805} (Pr)^{1/3}$$

$$= 0.027 (1.13 \times 10^5)^{0.805} (0.692)^{1/3}$$

$$= 279.1211$$

$$h = \frac{Nu \times k}{d} \left[\because Nu = \frac{hL}{k} \right]$$

$$= \frac{279.121 \times 0.03128}{0.05}$$

$$= 174.618 \text{ W/m}^2\text{C}$$

$$Q = hA \Delta t = h \times (\pi dL) (T_s - T_\infty)$$

$$= 174.618 \times \pi \times 0.05 (145 - 35)$$

$$= 3017.18 \text{ W}$$

5. Air at 1 atm & 35°C flow across a 5-cm diameter cylinder at a velocity of 50 m/s. The cylinder surface is maintained at a temp of 150°C. Calculate the heat loss per unit length of cylinder.

Sol Given data

$$T_i = 35^\circ\text{C}$$

$$T_o = 150^\circ\text{C}$$

$$D = 5\text{ cm} = 0.05\text{ m}$$

$$U = 50\text{ m/s}$$

$$T_f = \frac{T_i + T_o}{2} = \frac{35 + 150}{2} = 92.5^\circ\text{C}$$

The properties of air at 92.5°C

$$\rho = 0.966\text{ kg/m}^3$$

$$P_o = 0.695$$

$$k = 0.03\text{ W/mK}$$

$$\mu = 2.14 \times 10^{-5}\text{ kg/ms}$$

$$Re = \frac{\rho U D}{\mu}$$

$$= \frac{0.966 \times 50 \times 0.05}{2.14 \times 10^{-5}}$$

$$= 1.129 \times 10^5$$

$$Nu = \frac{hD}{k} = C_p (Re)^n (Pr)^{1/3}$$

$$Re = 1.1299 \times 10^5$$

$$Pr = 0.0266$$

$$n = 0.805$$

$$Nu = \frac{hD}{k} = C_p (Re)^{0.805} \times (Pr)^{1/3}$$

$$h = \frac{k}{D} \times 0.0266 \times (1.1299 \times 10^5)^{0.805} (0.697)^{1/3}$$

$$h = 165.271 \text{ W/m}^2\text{K}$$

$$Q = hA(T_o - T_i)$$

$$Q = h \pi \times D (T_o - T_i)$$

$$Q = (165.271) \times \pi \times (0.05) (150 - 35)$$

$$Q = 2985.47 \text{ W}$$

⑥ In an ice plant, liquid ammonia flows through a rectangular pipe of section 50 mm x 25 mm, at a velocity of 1 m/min & inlet temp of -30°C & leaves at 0°C . estimate HT coefficient & HT rate.

Sol $A = 30 \times 25$

$$u = 1 \text{ ml/min}$$
$$= 0.0166 \text{ m/s}$$

$$T_f = -30^\circ \text{C}$$

$$T_o = 0^\circ \text{C}$$

Properties of NH_3 at mean temp of -15°C .

$$\rho = 660 \text{ kg/m}^3$$

$$\nu = 0.3795 \times 10^{-6} \text{ m}^2/\text{s}$$

$$C_p = 4536.5 \text{ J/kg}\cdot\text{K}$$

$$k = 0.54485 \text{ W/m}\cdot\text{K}$$

$$L_c = \frac{4A_c}{P}$$

$$= \frac{4 \times 0.05 \times 0.025}{2(0.05 + 0.025)} = 0.033 \text{ m}$$

$$Re = \frac{L_c u}{\nu}$$

$$= \frac{0.033 \times 0.0166}{0.3795 \times 10^{-6}} = 1443.478$$

$$P_0 = \frac{\rho V C_p}{k}$$

$$= \frac{660 \times 0.3795 \times 10^{-6} \times 4536.5}{0.54485}$$

$$= 2085$$

$$Nu = \frac{hL_c}{k}$$

$$h = \frac{3.391 \times 0.54485}{0.033}$$

$$= 55.98 \text{ W/m}^2\text{K}$$

$$Q = m C_p \Delta T$$

$$= \rho \times A \times L \times C_p (T_0 - T_i)$$

$$\frac{Q}{L} = \rho A C_p (T_0 - T_i)$$

$$= 660 \times 0.05 \times 0.025 \times 4536.5 (0 - (-30))$$

$$= 112278.37 \text{ W}$$

⑦ Water at 50°C enters a 1.5 cm diameter 23 m long tube with a velocity of 1 m/s. The tube wall is maintained at a constant temp of 90°C . Calculate the HT coefficient & total amount of HT if the exit water temp is 64°C .

$$\text{Sol } A = \frac{\pi}{4} \times \left(\frac{1.5}{100}\right)^2$$
$$= 1.767 \times 10^{-4} \text{ m}^2$$

$$v = 1 \text{ m/s}$$

$$T_i = 50^\circ\text{C}$$

$$T_o = 64^\circ\text{C}$$

$$T_{\text{wall}} = 90^\circ\text{C}$$

Properties of H_2O at 50°C

$$\rho = 990 \text{ kg/m}^3$$

$$\gamma = 0.567 \times 10^{-6} \text{ m}^2/\text{s}$$

$$\alpha = 0.1532 \times 10^{-6} \text{ m}^2/\text{s}$$

$$Pr = 2.18$$

$$C_p = 4180.5 \text{ J/kg}\cdot\text{K}$$

$$k = 1.2793 \text{ W/m}\cdot\text{K}$$

$$\mu = \gamma \times \rho = 5.67 \times 10^{-6} \times 990$$

$$= 5.6133 \times 10^{-4} \text{ N}\cdot\text{s/m}^2$$

$$Re = \frac{\rho v d}{\mu}$$

$$= \frac{990 \times 1 \times \frac{1.5}{100}}{5.6133 \times 10^{-4}} = 2.6455 \times 10^4$$

$$5.6133 \times 10^{-4}$$

$$Nu = 0.332 Re^{0.5} \cdot Pr^{0.333}$$

$$= 0.332 \times (2.6455 \times 10^4)^{0.5} \times (2.18)^{0.333}$$

$$= 70$$

The only driving force in free convection is the buoyancy force out of which a flow field exists, without the presence of any external field.

The ratio of buoyancy force to the viscous force in the fluid is termed as the Grashoff No.

This number plays a significant role in free convection in a similar way as Reynolds no in forced convection.

when both free & forced convections occur simultaneously.

$$Nu = f(Re, Pr, Gr)$$

where

$Nu \rightarrow$ Nusselt no.

$Re \rightarrow$ Reynolds no.

$Pr \rightarrow$ prandtl no.

$Gr \rightarrow$ Grashoff no.

What is the criterion for transition from laminar to turbulent flow in free convective HT?

Ans The transition from laminar to turbulent flow in free convection boundary layers occurs when the value of $Gr \cdot Pr$ (Ra) approaches 10^9 .

$$Ra_L = Gr \cdot Pr = \frac{g \beta L^3 (T_s - T_\infty)}{\nu^2} \times Pr = 10^9.$$

where

β coefficient of thermal expansion,

L length of the plate, m.

T_s surface temp, $^{\circ}C$.

T_∞ = Ambient temp, $^{\circ}C$.

ν = kinematic viscosity, m^2/s

Pr = Prandtl number

Gr = Grashoff's no.

Ra_L = Rayleigh number

Grashoff no significance in natural convective

HT:-

D. A vertical cylinder 1.8m high and 7.5cm in diameter is maintained at a temperature of 93°C in an atmospheric air of 30°C . Calculate the heat loss by free convection from this cylinder.

Sol Given Data.

$$L = 1.8\text{m}$$

$$D = 7.5\text{cm} = 0.075\text{m}$$

$$T_s = 93^{\circ}\text{C}$$

$$T_{\infty} = 30^{\circ}\text{C}$$

$$T_f = \frac{T_s + T_{\infty}}{2} = \frac{93 + 30}{2} = 61.5^{\circ}\text{C}$$

Physical properties at 61.5°C .

$$\rho = 1.055\text{kg/m}^3$$

$$\nu = 19.1275 \times 10^{-6}\text{m}^2/\text{s}$$

$$\mu = 20.17 \times 10^{-6}\text{Ns/m}^2$$

$$P_r = 0.6957$$

$$C_p = 1005.6\text{J/kg}\cdot\text{K}$$

$$k = 0.02911\text{W/m}\cdot\text{K}$$

$$\beta = \frac{1}{T_f}$$

$$\beta = \frac{1}{T_f + 273} \Rightarrow \frac{1}{61.5 + 273} = 2.989 \times 10^{-3}$$

$$Gr_D = \frac{L^3 g \beta \Delta T}{\nu^2}$$

$$Gr_D = \frac{(1.8)^3 \times 9.81 \times 2.989 \times 10^{-3} \times (93 - 30)}{(19.1275 \times 10^{-6})^2}$$

$$Gr_D = 2.94 \times 10^{10}$$

$$Pr_D = 0.6957$$

$$Gr_D \cdot Pr_D = 2.94 \times 10^{10} \times 0.6957 \\ = 2.045 \times 10^{10}$$

$$Nu = \frac{hL}{k} = 0.1 (Gr_D Pr_D)^{1/3} \quad [10^9 < Gr_D Pr_D < 10^{12}]$$

$$h = \frac{k}{L} \times 0.1 (Gr_D \cdot Pr_D)^{1/3}$$

$$= \frac{0.02911}{1.8} \times 0.1 (2.045 \times 10^{10})^{1/3}$$

$$= 4.422 \text{ kJ/h m}^2 \text{ } ^\circ\text{C}$$

$$Q = hA\Delta T$$

$$\Rightarrow 4.422 \times (\pi \times 0.075 \times 1.8) (93 - 30)$$

$$= 118.15 \text{ kJ/h}$$

② The surface of human body may be approximated by a vertical cylinder 0.3 m in diameter 2.2 m in height. Assuming the surface temperature to be 30°C. Determine the heat loss from a human body in a quiescent atmosphere of air at 20°C. Use the appropriate correlation.

Sol Given Data.

$$d = 0.3 \text{ m}$$

$$h = 2 \text{ m}$$

$$T_s = 30^\circ\text{C}$$

$$T_\infty = 20^\circ\text{C}$$

$$T_f = \frac{T_s + T_\infty}{2}$$

$$= \frac{30 + 20}{2}$$

$$= \frac{50}{2}$$

$$\boxed{T_f = 25^\circ\text{C}}$$

properties of air at 25°C.

$$\rho = 1.184 \text{ kg/m}^3$$

$$k = 0.02581 \text{ W/m}\cdot\text{K}$$

$$\nu = 1.562 \times 10^{-5} \text{ m}^2/\text{s}$$

$$Pr = 0.7296$$

$$\beta = \frac{1}{T_f}$$

$$= \frac{1}{25 + 273}$$

$$= \frac{1}{298} = 0.003$$

$$\beta = 3 \times 10^{-3} \text{ K}^{-1}$$

$$Gr_D = \frac{g \beta (T_s - T_\infty) D^3}{\nu^2}$$

$$= \frac{(9.81) \times 3 \times 10^{-3} \times (30 - 20) (0.12)^3}{(1.562 \times 10^{-5})^2}$$

$$Gr_D = 9.649 \times 10^9$$

$$Nu = \frac{hL}{k} = 0.12 \times (Gr_D \cdot Pr)^{1/3}$$

$$= 0.12 \times (9.649 \times 10^9 \times 0.7296)^{1/3}$$

$$Nu = 229.46$$

$$Nu = \frac{hL}{k}$$

$$h = \frac{k \times Nu}{L}$$

$$= \frac{0.02551 \times 229.46}{2}$$

$$h = 2.926 \approx 3 \text{ W/m}^2\text{K}$$

$$h = 3 \text{ W/m}^2\text{K}$$

$$Q = hA \Delta T$$

$$= hA (T_s - T_\infty)$$

$$Q = 3 \times (\pi \times 0.3 \times 2) (30 - 20)$$

$$Q = 56.549 \text{ W}$$

③ A hot square plate of $75 \text{ cm} \times 75 \text{ cm}$ at 120°C is exposed to atmospheric air at 40°C . Find the heat loss from both sides of the plate if it is kept in

(i) Vertical position

(ii) Horizontal "

Sol Given Data.

$$A = 0.75 \times 0.75 = 0.5625 \text{ m}^2$$

$$T_s = 120^\circ \text{C}$$

$$T_\infty = 40^\circ \text{C}$$

$$T_f = \frac{T_s + T_\infty}{2}$$

$$= \frac{120 + 40}{2}$$

$$= \frac{160}{2} = 80^\circ\text{C}$$

Properties of air at 80°C ,

$$\gamma = 21.09 \times 10^{-6} \text{ m}^2/\text{Sec}$$

$$k = 0.03047 \text{ W/m}\cdot\text{K}$$

$$\rho = 1 \text{ kg/m}^3$$

$$Pr = 0.0692$$

$$g = 9.81 \text{ m/sec}^2$$

$$\beta = \frac{1}{T_f}$$

$$T_f = \frac{1}{T_s + T_\infty} = \frac{1}{80 + 273} = 2.8328 \times 10^{-3} \text{ K}^{-1}$$

(i) If plate is kept vertical

$$Gr = \frac{g \beta L^3 \Delta T}{\nu^2}$$

$$Gr = \frac{9.81 \times 2.8328 \times 10^{-3} \times (0.75)^3 \times 80}{(21.09 \times 10^{-6})^2}$$

$$Gr = 2.108 \times 10^9$$

$$Ra = (Gr \cdot Pr)$$

$$= 2.108 \times 10^9 \times 0.0692 \Rightarrow Ra = 1.459 \times 10^9$$

$$Ra = 1.459 \times 10^9 \geq 10^9$$

∴ flow is turbulent.

$$Nu = 0.125 (Ra)^{0.33}$$

$$Nu = 0.125 (1.459 \times 10^9)^{0.33}$$

$$Nu = 132.15$$

$$Nu = \frac{hL}{k} \Rightarrow h = Nu \cdot \frac{k}{L} = \frac{132.15 \times 0.03047}{0.75}$$

$$h = 5.368 \text{ W/m}^2\text{-K}$$

$$Q = hA \Delta t$$

$$= 5.368 \times (0.75)^2 \times 80$$

$$Q = 241.56 \text{ W}$$

$$Q = 0.24 \text{ kW}$$

(ii) If plate is kept at horizontal

for $Ra \geq 7 \times 10^8$ (turbulent)

$$Nu = 0.107 (Ra)^{0.33}$$

$$Nu = 113.12$$

$$\overline{h} = \frac{Nu \cdot k}{(A/P)}$$

$$\overline{h} = \frac{113.12 \times 0.03047}{\left(\frac{0.75}{2}\right)} = 9.19 \text{ W/m}^2\text{-K}$$

④ A vertical plate 5m high & 1.5m wide has one of its surfaces insulated. The other surface is maintained at a uniform temp of 400K & is exposed to quiescent atmospheric air at 300K. Calculate the total rate of heat loss from the plate. Properties of air at 350K are $\nu = 20.75 \times 10^{-6} \text{ m}^2/\text{s}$, $\rho = 0.697$ & $k = 0.03 \text{ W/mK}$

Sol Given Data.

$$h = 5 \text{ m}$$

$$b = 1.5 \text{ m}$$

$$T_s = 400 \text{ K}$$

$$T_\infty = 300 \text{ K}$$

$$T_f = \frac{400 + 300}{2}$$

$$= 350 \text{ K}$$

Properties of air at 350K.

$$v = 20.75 \times 10^{-6} \text{ m}^2/\text{s}$$

$$Pr = 0.697$$

$$k = 0.03 \text{ W/mK}$$

$$\beta = \frac{1}{T_f}$$

$$\beta = \frac{1}{350} = 2.8 \times 10^{-3}$$

$$Ra = \frac{g \beta \Delta t l^3}{\nu^2} \times Pr$$

$$= \frac{9.81 \times 2.8 \times 10^{-3} \times (400 - 300) \times 5^3}{(20.75 \times 10^{-6})^2} \times 0.697$$

$$= 5.5 \times 10^{11}$$

$Ra > 10^9$, \therefore flow is turbulent.

$$Nu = 0.125 Ra^{0.33}$$

$$= 0.125 \times (5.5 \times 10^{11})^{0.33}$$

$$= 935.9$$

$$Nu = \frac{hL}{k}$$

$$hc = \frac{935.9 \times 0.03}{5}$$

$$= 5.615 \text{ W/m}^2\text{K}$$

$$Q = h A \Delta t$$

$$Q = h A (T_s - T_\infty)$$

$$= 5.615 \times 5 \times 1.5 (400 - 300)$$

$$= 4.2 \times 10^3 \text{ W}$$

⑤. A vertical plate 20 cm x 60 cm size is at 110°C in an atmosphere at 30°C. Determine the rate of heat transfer by free convection from the plate when 20 cm side is kept vertical.

Sol $A = 20 \text{ cm} \times 60 \text{ cm}$

$$T_f = \frac{110 + 30}{2} = 70^\circ \text{C}$$

Physical properties at 70°C.

$$k = 0.02966 \text{ W/mK}$$

$$\nu = 20.02 \times 10^{-6} \text{ m}^2/\text{s}$$

$$P_r = 0.694$$

$$\beta = \frac{1}{t_f} = \frac{1}{70 + 273} = 2.9 \times 10^{-3}$$

$$Gr_D = \frac{L^3 \rho \beta \Delta T}{\nu^2}$$

$$L = 20 \text{ cm} \\ = 0.2 \text{ m}$$

$$Gr_D = \frac{(0.2)^3 \times 9.8 \times 2.9 \times 10^{-3} \times (110 - 30)}{(20 \cdot 0.2 \times 10^{-6})^2} \\ = 4.54 \times 10^7$$

$Gr_D < 10^9$ hence flow is laminar

$$Nu = 0.677 (Pr_D)^{1/2} (0.952 + Pr_D)^{-1/4} (Gr_D)^{1/4}$$

$$= 0.677 (0.694)^{1/2} (0.952 + 0.694)^{-1/4} (4.54 \times 10^7)^{1/4} \\ = 5.65 \times 10^6$$

$$Nu = \frac{hL}{k}$$

$$h = \frac{Nu \times k}{L}$$

$$\Rightarrow \frac{5.65 \times 10^6 \times 0.02966}{0.2}$$

$$\Rightarrow 8.38 \times 10^5 \text{ W/m}^2\text{C}$$

$$Q = hA\Delta T$$

$$= 8.38 \times 10^5 \times (0.2 \times 0.6) \times (110 - 30)$$

$$= 8.04 \times 10^6 \text{ Watts}$$

⑥. A metal plate 0.71 m in height & 1.02 m in width forms the vertical wall of an oven. The temp of the plate is maintained at 230°C, where as the air outside the oven is at 23°C. Assuming the oven to be uninsulated compute the convection heat loss from the wall to the outside air.

Sol Given data.

$$H = 0.71 \text{ m}$$

$$W = 1.02 \text{ m}$$

$$T_{\infty} = 23^{\circ}\text{C}$$

$$T_s = 230^{\circ}\text{C}$$

$$T_f = \frac{T_s + T_{\infty}}{2}$$

$$= \frac{230 + 23}{2}$$

$$T_f = 126.5^{\circ}\text{C}$$

Properties of air at 126.5°C.

$$\rho = 0.876 \text{ kg/m}^3$$

$$\mu = 23.29 \times 10^{-6} \text{ N s/m}^2$$

$$\nu = 26.625 \times 10^{-6} \text{ m}^2/\text{s}$$

$$\alpha = 38.583 \times 10^{-6} \text{ m}^2/\text{s}$$

$$Pr = 0.685$$

$$k = 0.03413 \text{ W/mk}$$

$$\beta = \frac{1}{T_f}$$

$$= \frac{1}{126.5 + 273}$$

$$= 2.5031 \times 10^{-3} \text{ K}^{-1}$$

$$Gr = \frac{g \beta H^3 (T_s - T_\infty)}{\nu^2}$$

$$\Rightarrow \frac{9.81 \times 2.5031 \times 10^{-3} \times (0.7)^3 \times 207}{(26.625 \times 10^{-6})^2}$$

$$Gr = 2.566 \times 10^9$$

$$Ra = Gr \cdot Pr \Rightarrow 2.566 \times 10^9 \times 0.685$$

$$Ra = 1.757 \times 10^9 \quad (\because Ra > 10^9)$$

\(\therefore\) flow is turbulent

$$Nu = 0.10 (Gr \cdot Pr)^{0.333}$$

$$= 0.10 (1.757 \times 10^9)^{0.333}$$

$$= 119.81$$

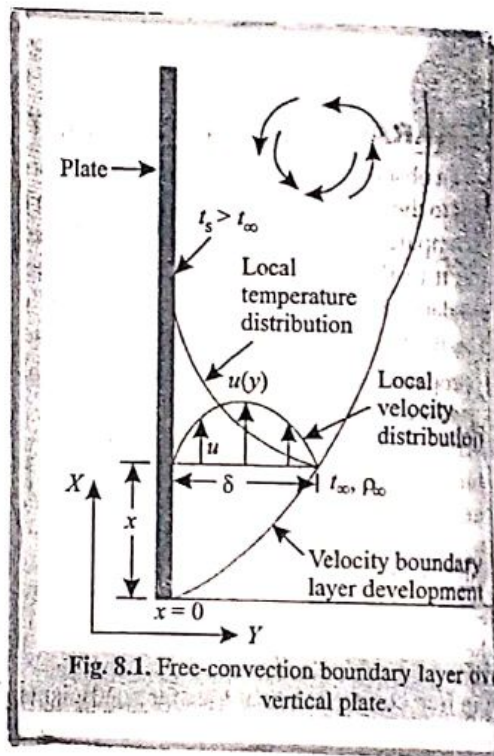
$$Nu = \frac{hL}{k}$$

$$h = \frac{Nu \times k}{H} = \frac{119.81 \times 0.03413}{0.7} \Rightarrow h = 5.759 \text{ W/m}^2\text{ }^\circ\text{C}$$

$$Q = hA\Delta t \quad [^\circ; A = WH]$$

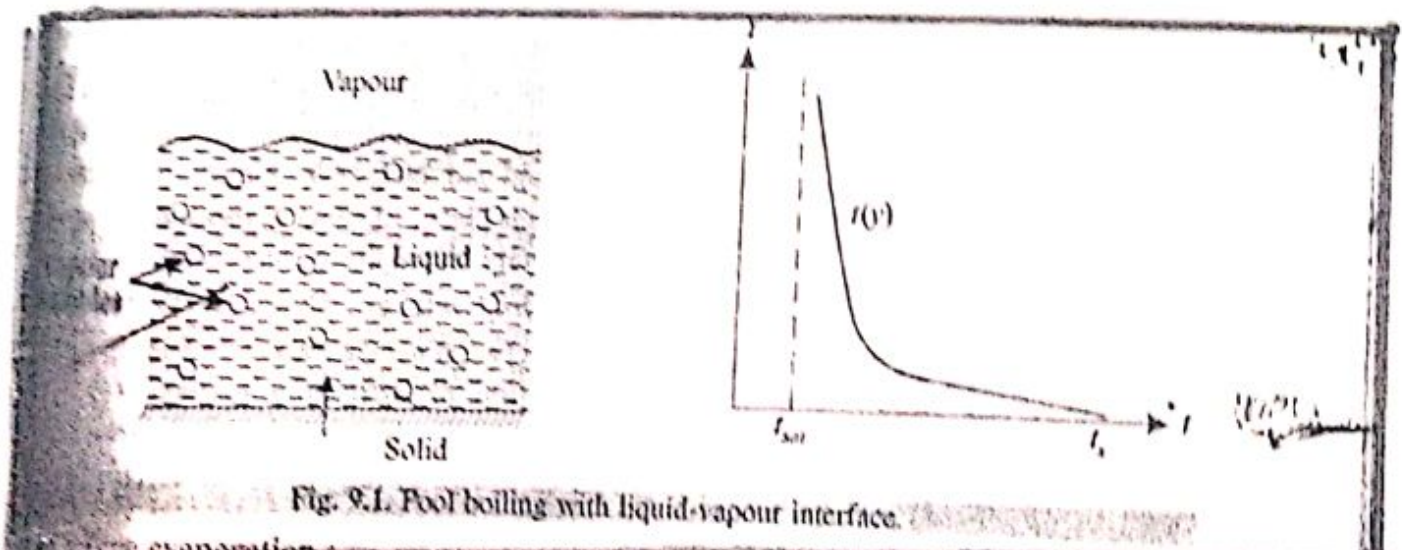
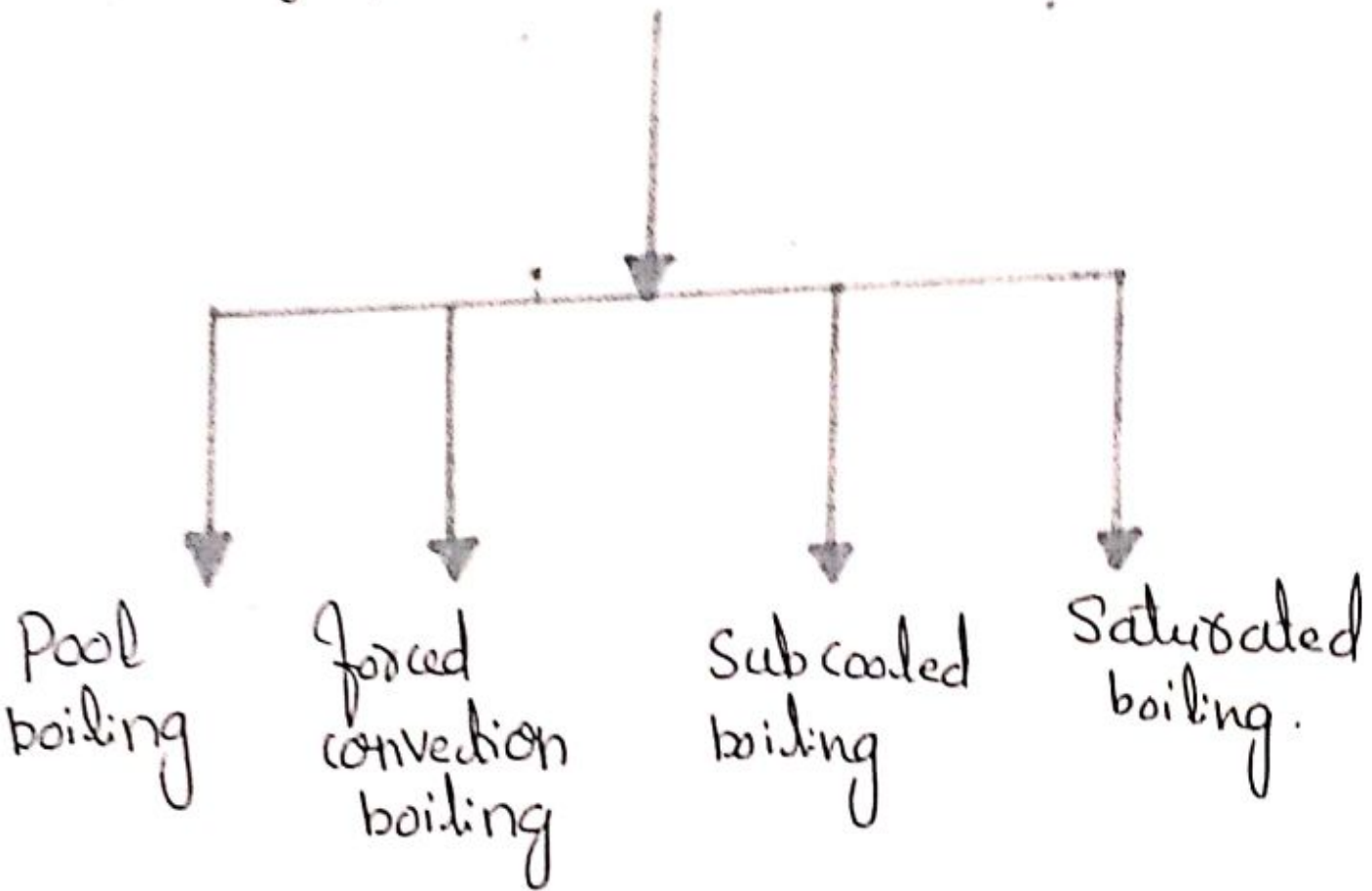
$$= 5.759 \times 0.71 \times 1.02 \times (230 - 23)$$

$$Q = 863.328 \text{ Watts}$$

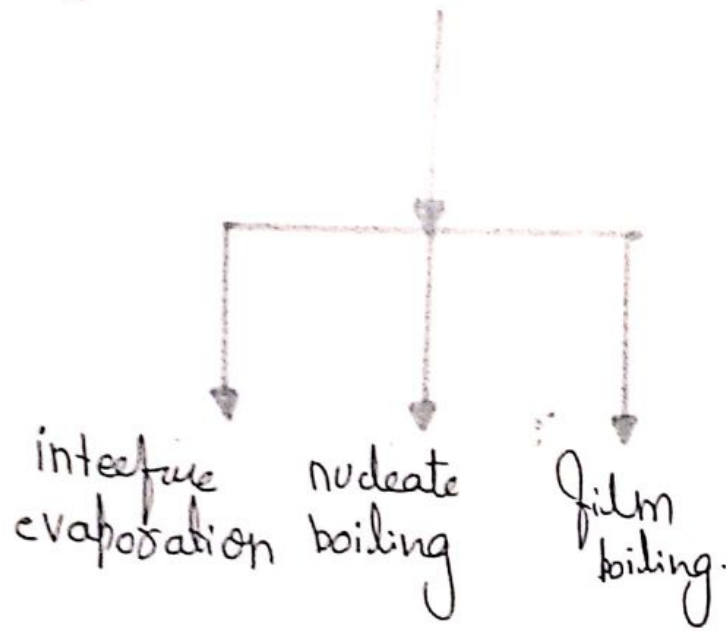


Boiling:- Boiling is a phase change from liquid to vapour state.

The boiling HT phenomenon may occur in the following forms.



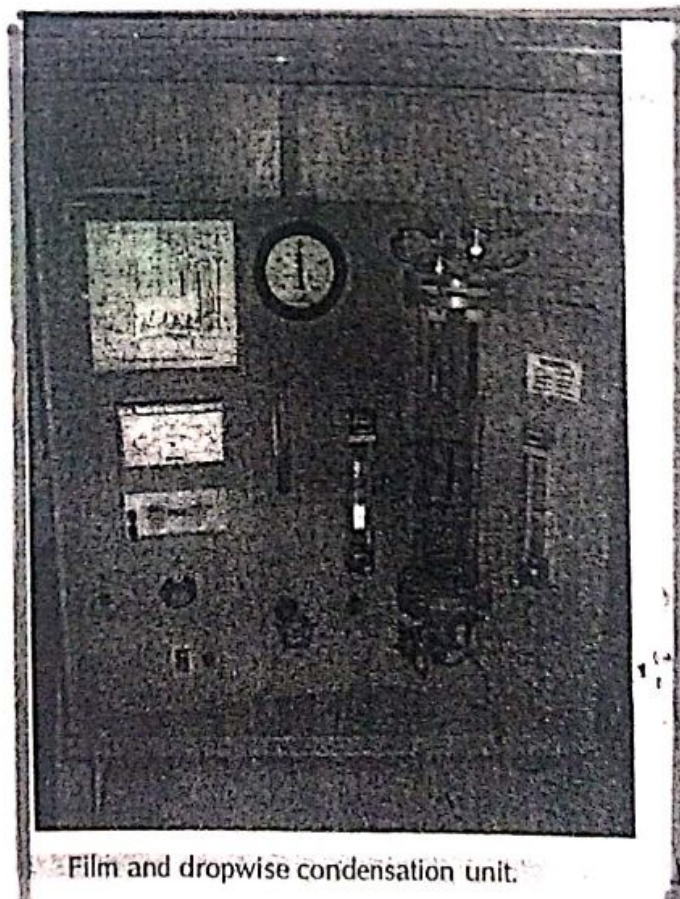
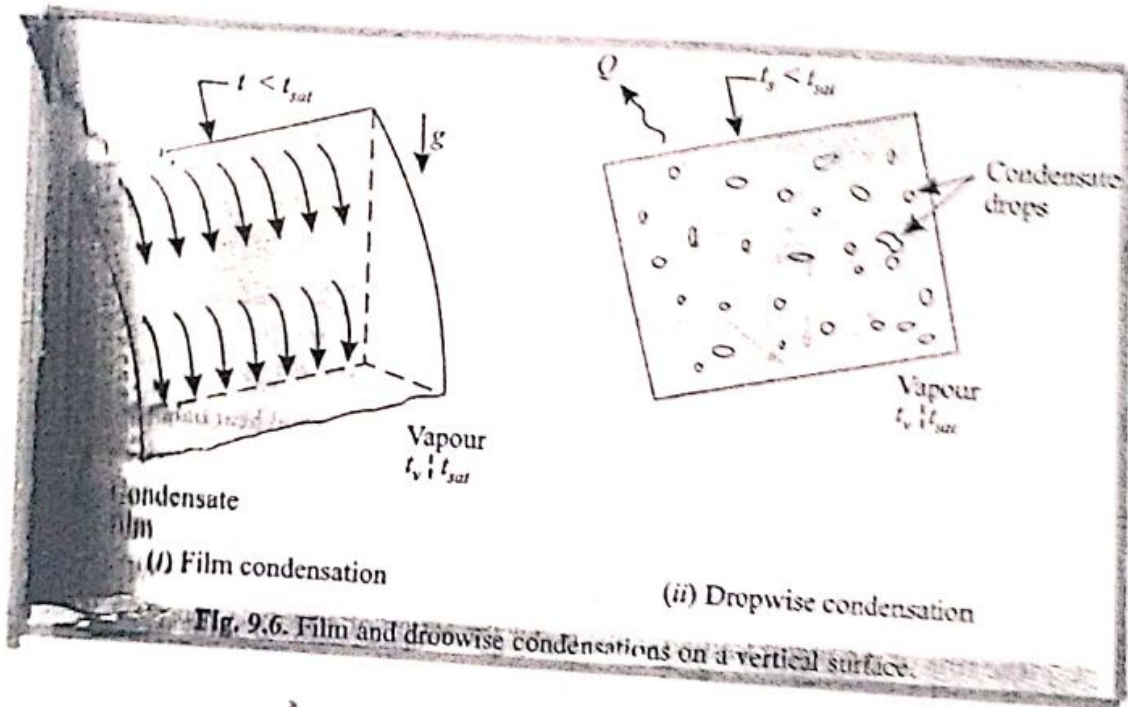
Boiling Regimes :- There are 3 regimes of Boiling



540

Condensation Process:- The condensation process is the reverse of boiling.

Liquid \rightarrow Solid.



D. Steam at atmospheric pressure & the tube surface temp is maintained at 98°C . What is the rate at which steam is condensed/unit length of the tubes.

Sol

$$T_s = 98^{\circ}\text{C}$$

$$T_{\text{sat}} = 100^{\circ}\text{C}$$

$$D = 1.27 \text{ mm}$$

$$= 1.27 \times 10^{-3} \text{ m}$$

$$T_f = \frac{T_s + T_{\text{sat}}}{2} = \frac{100 + 98}{2} = 99^{\circ}\text{C}$$

properties of condensate at this temp

$$\rho = 961 \text{ kg/m}^3$$

$$\nu = 0.293 \times 10^{-6} \text{ m}^2/\text{s}$$

$$\alpha = 0.168 \times 10^{-6} \text{ m}^2/\text{s}$$

$$P_r = 1.740$$

$$C_p = 4216 \text{ J/kg K}$$

$$k = 0.6804 \text{ W/m K}$$

$$u = \rho \times \nu = 2.8157 \times 10^{-8} \text{ kg/ms}$$

$$\lambda = 2074.7 \text{ kJ/kg}$$

$$h_{fg} = \frac{2258}{1000} \text{ kJ/kg}$$

$$N = \sqrt{100} = 10$$

The HT coefficient for tubes is given by

$$\bar{h} = 0.725 \left[\frac{\lambda \cdot \rho^2 L g k^3 h_{fg}}{4 D (\theta_{sat} - \theta_s) N} \right]^{1/4}$$

$$= 0.725 \left[\frac{2074.7 \times (961)^2 \times 1.27 \times 981 \times (0.6804)^3 \times 2258}{2.8157 \times 1.27 (100 - 98)} \right]^{1/4}$$

$$h =$$

- ② A heated polished copper plate is immersed in a pool of water boiling at atmospheric pressure. If the surface of the copper plate is maintained at a temp. of 123°C . Find the surface heat flux and the evaporation rate/unit area of the plate

Sol Given data.

$$T_{\text{sat}} = 100^\circ\text{C}$$

$$T_w = 125^\circ\text{C}$$

The properties of water at 100°C are

$$\rho_l = 961 \text{ kg/m}^3$$

$$C_p = 4216 \text{ J/kg}\cdot\text{K}$$

$$\lambda = 2256.6 \text{ kJ/kg}$$

$$\nu_l = 0.293 \times 10^{-6} \text{ m}^2/\text{s}$$

$$\mu = \rho \times \nu = 961 \times 0.293 \times 10^{-6}$$
$$\Rightarrow 2.815 \times 10^{-4} \text{ N}\cdot\text{s/m}^2$$

$$Pr = 1.740;$$

$$n = 1.7; k = 0.0013, \rho_v = 0.598 \text{ kg/m}^3$$

$$\sigma = 58.9 \times 10^{-3} \text{ N/m}$$

$$q = 4\lambda \sqrt{\frac{g(\rho_l - \rho_v)}{\sigma}} \times \left[\frac{C_p (T_w - T_{\text{sat}})}{k \cdot \lambda \cdot Pr^n} \right]^3$$

$$\Rightarrow \left[2.815 \times 10^{-4} \times 2256.6 \times 10^3 \times \sqrt{\frac{9.81(961 - 0.598)}{58.9 \times 10^{-3}}} \times \frac{4216(125 - 100)}{0.0013 \times 2256.6 \times 10^3 \times (1.740)^{1.7}} \right]^3$$
$$\Rightarrow 698.960 \times 10^6 \text{ kW/m}^2$$

Heat flux

$$q_v = 698.960 \times 10^6 \text{ kW/m}^2$$

Evaporation rate per unit area is

$$m = \frac{q_v}{\lambda}$$

$$\Rightarrow \frac{698.960 \times 10^6}{2256.6 \times 10^3}$$
$$= 309.74$$

③ Water at 5 bar flows inside a 25mm diameter tube under local boiling conditions where the tube wall temp is 15°C above the saturation temp. Estimate the HT in a 0.6m length of tube.

Sol

$$\Delta T_e = T_s - T_{\text{sat}}$$
$$= 15^\circ\text{C}$$

$$D = 25 \text{ mm}$$
$$= 0.025 \text{ m}$$

$$l = 0.6 \text{ m}$$

$$P = 5 \text{ bar}$$

$$= 5 \times (1.0132 \times 10^5)$$

$$= 5.066 \times 10^5 \text{ N/m}^2$$

$$= 0.5066 \times 10^6 \text{ N/m}^2$$

$$h = 2.54 (\Delta T_e)^3 \cdot e^{P/1.556}$$

$$\Rightarrow 2.54 (15)^3 \times e^{\frac{0.5066}{1.551}}$$

$$= 11883.9 \text{ W/m}^2\text{K}$$

HT in 0.6 m length of tube

$$Q = h A \Delta t$$

$$Q = h (\pi D L) \times \Delta t$$

$$= (11883.9) (\pi \times 0.025 \times 0.6) \times 15$$

$$= 8400.23 \text{ W}$$

⑤ A heated $30 \times 30 \text{ cm}$ square copper plate serves as the bottom for a pan of water at 1 atm pressure. The temp. of the plate is maintained at 119°C . Estimate the heat transfer per hour by the plate.

Sol Given Data.

$$T_s = 119^\circ\text{C}$$

$$T_{\text{sat}} = 100^\circ\text{C}$$

$$L = 30 \text{ cm}$$

$$= 0.3 \text{ m}$$

$$T_f = \frac{T_s + T_{sat}}{2}$$

$$= \frac{119 + 100}{2}$$

$$= 109.5^\circ\text{C}$$

Amount of condensate

$$M = \frac{\dot{Q}}{h_{fg}}$$

where, $\dot{Q} = h \cdot A (T_{sat} - T_s)$

At 109.5°C ,

properties of water,

$$\rho_l = 953 \text{ kg/m}^3$$

$$\nu = 0.274 \times 10^{-6} \text{ m}^2/\text{s}$$

$$\alpha = 0.1694 \text{ m}^2/\text{s}$$

$$Pr = 1.393$$

$$C = 4.233 \text{ J/kg}\cdot\text{K}$$

$$k = 0.6827 \text{ W/m}\cdot\text{K}$$

$$h_{fg} = 2237 \text{ kJ/kg}$$

$$M_l = \rho \cdot V$$

$$\Rightarrow 2.573 \times 10^6 \text{ kg/m}^2$$

$$h = 0.953 \left[\frac{\rho_l^2 h_{fg} \times g \times k^3}{\mu_l (T_{sat} - T_s)} \right]^{1/4}$$

$$h = 0.953 \left[\frac{(0.953)^2 \times 2257 \times 9.81 \times (0.01827)^3}{0.3 \times 2.57 \times 10^{-8} (100 - 119)} \right]^{1/4}$$

$$h = -527.284 \text{ W/m}^2\text{K}$$

$$Q = hA \Delta t$$

$$Re = \frac{4hL(T_{sat} - T_s)}{h_{fg} \times \mu}$$

$$\Rightarrow \frac{4 \times (-16499.233) \times 0.3 \times (100 - 119)}{2257 \times 2.573 \times 10^{-8} \times 10^3}$$

$$= 2.07 \times 10^5$$

$$Q = hA \Delta t$$

$$= hA (T_{sat} - T_s)$$

$$\Rightarrow 527.284 \times 0.3^2 (100 - 119)$$

$$= 901.655 \text{ W}$$

Rate of Condensation/hy

$$M = \frac{Q}{h_{fg}} = \frac{901.655 \times 10^3}{2257} = 0.4 \text{ kg/h}$$

⑤ Saturated steam at ~~one~~ 1 atm. pressure condenses on a 3 m high & 4 m wide vertical plate that is maintained at 90°C by circulating cooling water through the other side. Determine

- The total rate of HT by condensation to the plate.
- The avg. HT coefficient over the entire plate.

Sol

$$L = 3 \text{ m}$$

$$W = 4 \text{ m}$$

$$A = 4 \times 3 = 12 \text{ m}^2$$

At 1 atm pressure

$$t_{\text{sat}} = 100^\circ\text{C}$$

$$h_{fg} = 2257 \times 10^3 \text{ J/kg}$$

$$t_\infty = 90^\circ\text{C}$$

$$t_f = \frac{t_{\text{sat}} + t_\infty}{2} = 95^\circ\text{C}$$

At 95°C , properties of water are

$$\rho = 964.5 \text{ kg/m}^3$$

$$k = 0.6775 \text{ W/mK}$$

$$\mu = 299.7 \times 10^{-6} \text{ kg/m-sec}$$

$$4) \quad h_v = 0.943 \left[\frac{k_f^3 \rho_f^2 g h_{fg}}{\mu_f L (T_{sat} - T_w)} \right]^{1/4} \quad \therefore \rho_f \ll \ll \ll \rho_g$$

$$h_v = 0.943 \left[\frac{(0.6775)^3 \times (964.5)^2 \times 9.81 \times 2257 \times 10^3}{299.7 \times 10^{-6} \times 3 \times (100 - 90)} \right]^{1/4}$$

$$= 4871.83 \text{ W/m}^2\text{K}$$

$$b) \quad Q = h A \Delta T$$

$$= 4.871 \times 12 \times (100 - 90)$$

$$= 584.62 \text{ kW}$$

6. Dry saturated steam at a pressure of 2.5 bars condenses on the surface of vertical tube of height 1.5m. The tube surface temp is 120°C. Estimate the thickness of condensate film & the local HT coefficient at a distance of 0.3m from the upper end of the tube.

Sol
Dry saturated steam at a pressure of 2.5 bars

$$T_g = 127.4^\circ\text{C}$$

$$h = 1.5\text{m}$$

$$T_w = 120^\circ\text{C}$$

$$\text{Thickness } (\delta) = ?$$

$$h = ?$$

$$\alpha = 0.3$$

$$T_f = \frac{127.4 + 120}{2}$$

$$= 123.7^\circ\text{C}$$

$$\rho = 941.855 \text{ kg/m}^3$$

$$k = 0.6847 \text{ W/mK}$$

$$C = 4256.105 \text{ J/kg-K}$$

$$u = \rho \cdot \delta \cdot v$$

$$= 941.85 \times 0.24 \times 10^{-6}$$

$$= 2.26 \times 10^{-4} \text{ kg/ms}$$

$$h_{fg} \text{ at } 127.4^\circ\text{C} = 2781 \text{ kJ/kg}$$

$$e_v = \frac{1}{0.781}$$

$$= 1.39 \text{ kg/m}^3$$

$$\delta = \left[\frac{4 \alpha k \alpha (T_g - T_w)}{g h_{fg} (\rho_l - \rho_v) \rho_l} \right]^{1/4}$$

$$\Rightarrow \left[\frac{4 \times 2.26 \times 10^{-4} \times 0.6847 \times 0.3 \times (127.4 - 120)}{9.81 \times 218 \times 10^3 \times 941.85 (941.85 - 1.39)} \right]^{0.25}$$

$$= 9.227 \times 10^{-5}$$

$$\text{But, } G = \frac{\rho_l (\rho_l - \rho_v) \times g \times \delta^3}{3 \mu}$$

$$= \left[\frac{941.85 (941.85 - 1.39) \times 9.81}{3 \times 2.26 \times 10^{-4}} \right] \times (9.227 \times 10^{-5})^3$$

$$= 0.01 \text{ kg/m width}$$

$$\text{Re} = \frac{4G}{\mu}$$

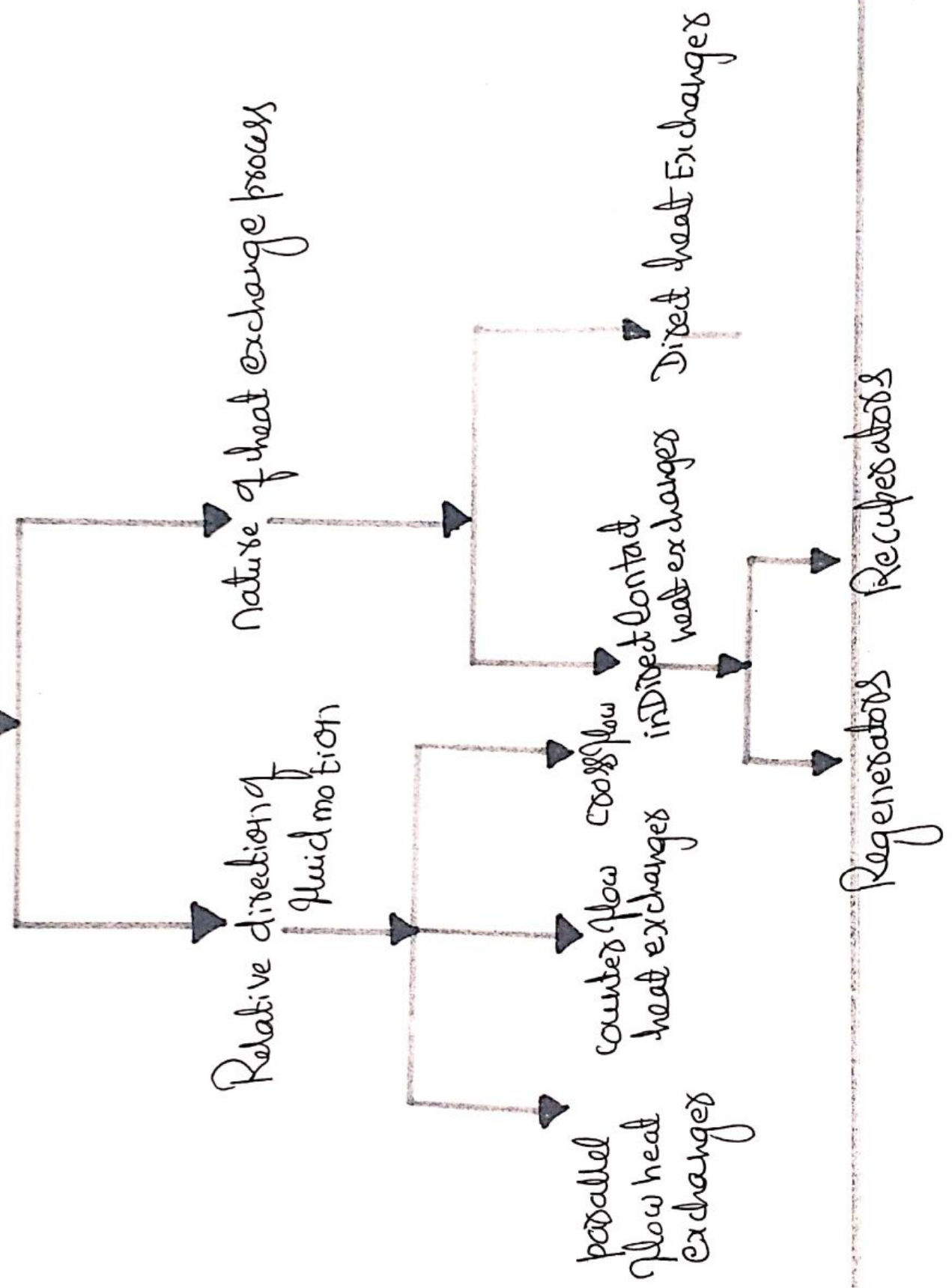
$$= \frac{4 \times 0.01}{2.26 \times 10^{-4}} = 176.99$$

$$h = \left[\frac{\rho_l (\rho_l - \rho_v) g \times h_{fg} \times k^3}{4 \mu \times (T_g - T_w)} \right]^{1/4}$$

$$\Rightarrow \left[\frac{941.85 (941.85 - 1.39) \times 9.81 \times 2181 \times 10^3 \times (0.6847)^3}{4 \times 2.26 \times 10^{-4} \times 0.3 (127.4 - 120)} \right]^{1/4} \quad \cdot 25$$

$$h = 7420.045 \text{ W/m}^2\text{K}$$

CLASSIFICATION OF HEAT EXCHANGERS



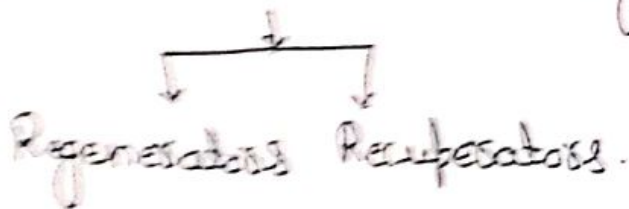
Classification of heat exchangers :-

I- Relative direction of fluid motion.

- a) Parallel flow heat exchangers.
- b) Counter flow heat exchangers.

- nature of heat exchange process.

- a) Direct contact heat exchangers
- b) Indirect contact heat exchangers



Differences b/w parallel & counter flows.

Parallel flow heat exchanger	Counter flow heat exchanger
<p>The 2 fluid streams (hot & cold) travel in same direction and is smaller.</p> <p>Requires more area for heat transfer.</p> <p>The 2 fluids enter at one end and leave at the other end.</p> <p>The temp. difference b/w the hot & cold fluids goes on decreasing in inlet to outlet.</p>	<p>The 2 fluids travel in opposite direction.</p> <p>① LMTD is greater.</p> <p>② Requires less area for heat transfer.</p> <p>③ The hot and cold fluids enter at opposite directions.</p> <p>④ The temp. difference b/w 2 fluids remains more or less nearly constant.</p>

FOULING:- The phenomenon of rust formation and deposition of fluid impurities is called fouling.

It results in a lower overall heat transfer coefficient in operation than that calculated for clean surfaces.

Due to fouling effect, the effectiveness of heat exchange may be greatly reduced.

An allowance is often made for scaling and fouling in design of heat exchangers by assigning "fouling factors" to surfaces which will become coated in use.

The fouling factor for any given scaling or fouling is equal to the thermal resistance of scale. The magnitude of fouling factors depends on the nature of the scale. If the scale is in uniform in composition and structure, the resistance may be calculated by ~~calculating~~ dividing the thickness of the scale to ~~thermal~~ conductivity of the scale material.

However, the scale is usually of unknown or complicated composition and structure.

Fouling factors are determined experimentally by testing the heat exchangers in both clean and dirty conditions.

$$R_f = \frac{1}{u_{\text{dirty}}} - \frac{1}{u_{\text{clean}}}$$

where, $u_{\text{dirty}} \rightarrow$ overall heat transfer coefficient of dirty surface.

$u_{\text{clean}} \rightarrow$ overall heat transfer coefficient of clean surface.

ANALOGY B/W HEAT, MASS & MOMENTUM TRANSFER:-

The mathematical laws governing momentum, heat & mass transfers are similar. \therefore heat, mass and momentum transfer equations for the boundary layers can be written as.

$$\frac{\partial \psi}{\partial x} + \frac{\partial \psi}{\partial y} = 0$$

heat transfer,

$$u \cdot \frac{\partial T}{\partial x} + v \cdot \frac{\partial T}{\partial y} = \alpha \cdot \frac{\partial^2 T}{\partial y^2}$$

mass transfer,

$$u \cdot \frac{\partial C_a}{\partial x} + v \cdot \frac{\partial C_a}{\partial y} = D \cdot \frac{\partial^2 C_a}{\partial y^2}$$

Momentum Transfer,

$$u \cdot \frac{\partial u}{\partial x} + v \cdot \frac{\partial u}{\partial y} = \nu \cdot \frac{\partial^2 u}{\partial y^2}$$

$$Pr = \frac{\nu}{\alpha} = 1$$

$$Sc = \frac{\nu}{D} = 1$$

$$Le = \frac{\nu}{D} = 1$$

$$Pr = Sc = Le = 1$$

A double pipe heat exchanger is constructed of a stainless steel ($k = 151 \text{ W/mK}$) inner tube of $D_i = 15 \text{ mm}$ and $D_o = 19 \text{ mm}$ & the outer tube of dia 32 mm . The convective HT coefficient is given to be $h_i = 800 \text{ W/m}^2\text{K}$ & $h_o = 1200 \text{ W/m}^2\text{K}$. For a fouling factor $R_{fi} = 0.0004 \text{ m}^2\text{K/W}$ on the tube side & $R_{fo} = 0.0001 \text{ m}^2\text{K/W}$ on shell tube, determine.

(i) Total thermal resistance

(ii) U_i

(iii) U_o

$$D_o = 15 \text{ mm}$$

$$D_i = 7.5 \text{ mm}$$

$$D_o = 14 \text{ mm}$$

$$D_o = 7.5 \text{ mm}$$

$$h_i = 800 \text{ W/m}^2\text{K}$$

$$h_o = 1200 \text{ W/m}^2\text{K}$$

$$R_{fi} = 0.0004 \text{ m}^2\text{K/W}$$

$$R_{fo} = 0.0001 \text{ m}^2\text{K/W}$$

$$k_{\text{of stainless}} = 15.1 \text{ W/mK}$$

$$\begin{aligned} (1) \quad R_s &= \frac{\ln(D_o/D_i)}{2\pi k} \\ &= \frac{\ln\left(\frac{9.5}{7.5}\right)}{2\pi (15.1)} \end{aligned}$$

$$= 2.49 \times 10^{-3}$$

$$= 0.00249$$

Resistance on inside

$$R_i = \frac{1}{h_i A_i} = \frac{1}{h_i 2\pi r_i^2}$$

$$= \frac{1}{1200 \times 2\pi \times 9.5 \times 10^{-3}} = 0.01396$$

$$\text{Total Resistance} = R_s + R_i + R_o$$

$$= 0.04297$$

(ii) U_i

$$U_i = \frac{1}{\frac{1}{h_i} + R_{fi} \left[\frac{\delta_i}{k} \right] \ln \left[\frac{\delta_o}{\delta_i} \right] + \left[\frac{\delta_i}{\delta_o} \right] R_{fo} + \left[\frac{\delta_i}{\delta_o} \right] \left[\frac{1}{h_o} \right]}$$

$$\Rightarrow \frac{1}{\frac{1}{800} + (0.0004) \left[\frac{7.5}{15.1} \right] \ln \left[\frac{9.5}{7.5} \right] + \left[\frac{7.5}{9.5} \right] 0.0001 + \left[\frac{7.5}{9.5} \right] \left[\frac{1}{1200} \right]}$$

\Rightarrow

$$U_i = \frac{1 \times 10^4}{20.3375}$$

$$= 0.049170252 \times 10^4$$

$$= 491.702 \text{ W/m}^2\text{K}$$

$$= 491.702 \text{ W/m}^2\text{K}$$

(iii)

$$U_o = \frac{1}{\frac{1}{h_o} + R_{fo} \left[\frac{\delta_o}{k} \right] \ln \left[\frac{\delta_o}{\delta_i} \right] + \left[\frac{\delta_o}{\delta_i} \right] R_{fi} + \left[\frac{\delta_o}{\delta_i} \right] \left[\frac{1}{h_i} \right]}$$

$$\Rightarrow \left[\frac{1}{1200} \right] + \left[(0.0001) \left[\ln \left(\frac{9.5}{7.5} \right) \right] \times \frac{9.5}{15.1} \right] + \left[\left[\frac{9.5}{7.5} \right] \times (0.0004) \right]$$

$$+ \left[\left[\frac{9.5}{7.5} \right] \times \frac{1}{800} \right]$$

$$= 0.034039 \times 10^4$$

$$= 340.3942 \text{ W/m}^2\text{K}$$

② Determine the overall HT coefficient based on the outer area of a 3.81 cm O.D & 3.175 cm I.D brass ($K = 103.8 \text{ W/mK}$) if the HT coefficient for flow inside & outside the tube are 2270 & 2840 $\text{W/m}^2\text{K}$ & the unit fouling resistances at inside & outside are $R_{fi} = R_{fo} = 0.0088 \text{ m}^2\text{K/W}$.

Sol

$$d_i = 3.175 \text{ cm} = 0.0317 \text{ m}$$

$$d_o = 3.81 \text{ cm} = 0.0381 \text{ m}$$

$$K = 103.8 \text{ W/mK}$$

$$h_i = 2270 \text{ W/m}^2\text{K}$$

$$h_o = 2840 \text{ W/m}^2\text{K}$$

$$R_{fi} = R_{fo} = 0.0088 \text{ m}^2\text{K/W}$$

Overall HT coefficient is

$$\frac{1}{U_o} = \left[\frac{d_o}{d_i} \times \frac{1}{h_i} \right] + \left[\frac{d_o}{d_i} \times R_{fi} \right] + \left[\frac{d_o}{K} \times \ln \left(\frac{d_o}{d_i} \right) \right] + R_{fo} + \frac{1}{h_o}$$

$$\frac{1}{U_0} = 5.294 \times 10^{-4} + 0.0105 = 10^{-4} \left[5.294 + 10.5 \right] \text{ (W/m}^2\text{K)} \\ + 3.5211 \times 10^{-4} + 0.0105$$

$$\frac{1}{U_0} = 202.918 \times 10^{-4}$$

$$U_0 = 49.2808 \text{ W/m}^2\text{K}$$

③ A heat exchanger is required to cool 5000 kg/h of alcohol from 65°C to 40°C using water at 15°C entering at 5°C. Calculate the temperature difference for

(i) parallel flow

(ii) counter flow

Take $U = 580 \text{ W/m}^2\text{K}$, $C_{p, \text{alcohol}} = 4180 \text{ J/kg}\cdot\text{K}$

$$C_{p, \text{water}} = 3760 \text{ J/kg}\cdot\text{K}$$

Sol

$$C_{p, \text{alcohol}} = 4180 \text{ J/kg}\cdot\text{K}$$

$$C_{p, \text{water}} = 3760 \text{ J/kg}\cdot\text{K}$$

$$U = 580 \text{ W/m}^2\text{K}$$

$$m_h = \frac{55000}{3600} = 15.28 \text{ kg/s}$$

$$m_c = \frac{40000}{3600}$$

$$= 11.11 \text{ kg/s}$$

$$t_{h1} = 66^\circ\text{C}$$

$$t_{h2} = 40^\circ\text{C}$$

$$t_{c1} = 5^\circ\text{C}$$

$$Q = m_h C_{p_h} (t_{h1} - t_{h2})$$

$$= 15.277 \times 3760 (66 - 40)$$

$$= 11.11$$

$$t_{c2} = \left[\frac{15.277 \times 3760 \times 26}{11.11 \times 4180} \right] + 5$$

$$t_{c2} = 37.15^\circ\text{C}$$

$$(i) \quad Q_m = \frac{Q_1 - Q_2}{\ln(Q_1/Q_2)} = \frac{(t_{h1} - t_{c1}) - (t_{h2} - t_{c2})}{\ln \left[\frac{(t_{h1} - t_{c1})}{(t_{h2} - t_{c2})} \right]}$$

$$Q_m = \frac{(66 - 5) - (40 - 37.156)}{\ln \left(\frac{66 - 5}{40 - 37.156} \right)} = 18.97^\circ\text{C}$$

$$Q = UA \Delta T_m$$

$$A = \frac{Q}{U \Delta T_m}$$

$$= \frac{m_c C_{p,c} (t_{c2} - t_{c1})}{U \Delta T_m}$$

$$= \frac{11.111 \times 4180 \times (37.156 - 5)}{580 \times 18.9}$$

$$= 135.72 \text{ m}^2$$

(ii) Counter flow mode

$$\Delta T_m = \frac{\Delta T_1 - \Delta T_2}{\ln(\Delta T_1 / \Delta T_2)}$$

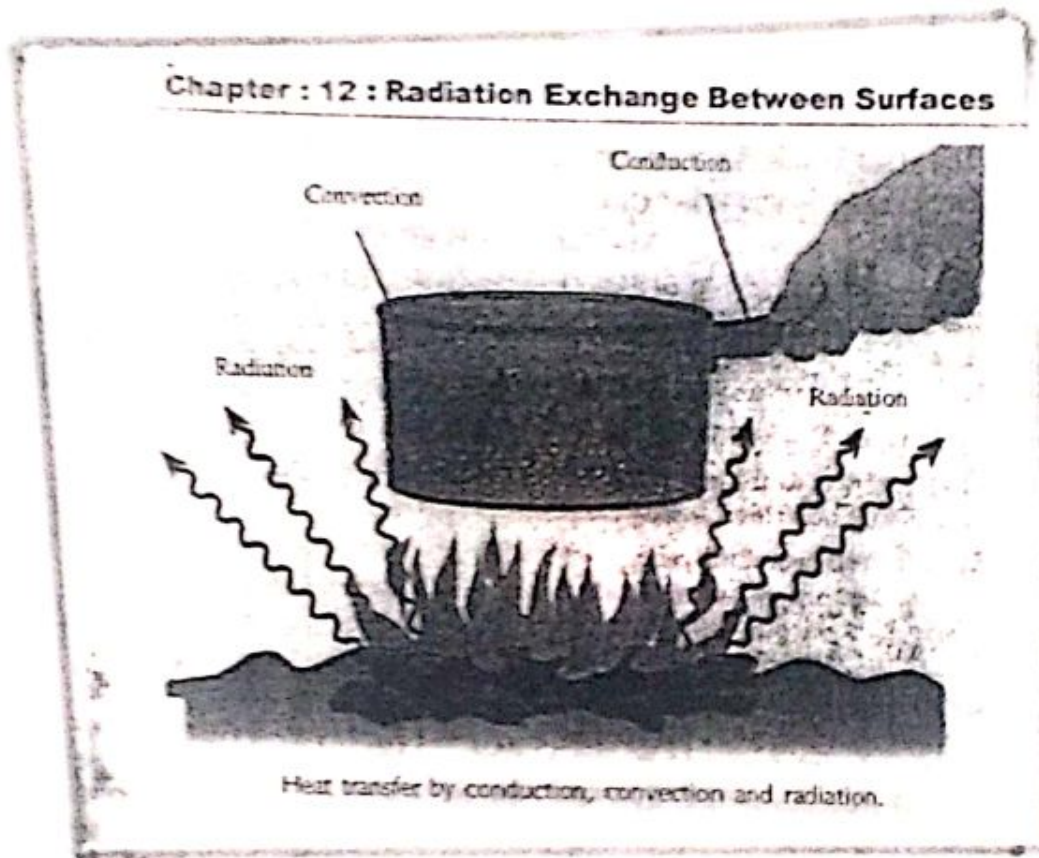
$$= \frac{(t_{h1} - t_{c2}) - (t_{h2} - t_{c1})}{\ln(t_{h1} - t_{c2} / t_{h2} - t_{c1})}$$

$$\Rightarrow \frac{(66 - 37.156) - (40 - 5)}{\ln\left(\frac{66 - 37.156}{40 - 5}\right)}$$

$$= \frac{32.844}{-0.1934}$$

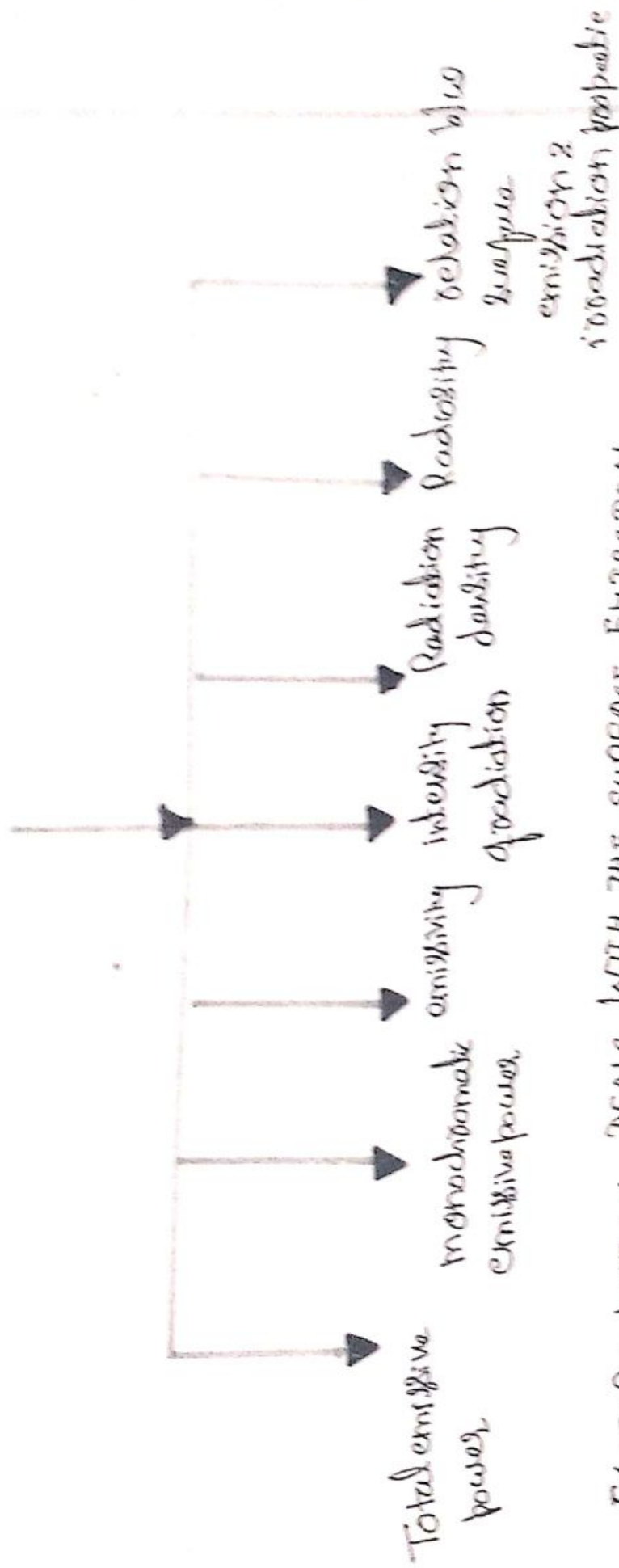
$$= 31.8304$$

Radiation:- The transfer of energy across a system by means of an electromagnetic waves.



The rate of emission of radiation by a body depends on the following.

- (i) Temperature of the surface.
- (ii) nature " " "
- (iii) wavelength



FACTORS WHICH DEALS WITH THE SURFACE EMISSION PROPERTIES ARE GIVEN BELOW

Black body:- Black body is one which neither reflects nor transmits any part of incident radiation.

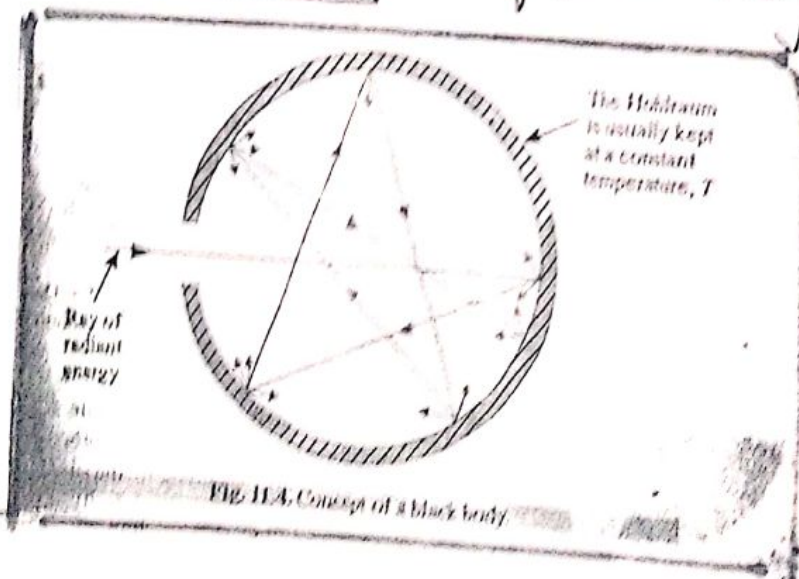
$$\boxed{\alpha=1, \rho=0, \tau=0} \rightarrow \text{for black body}$$

opaque body:- when no incident radiation is transmitted through the body is called an opaque body

$$\boxed{\tau=0, \alpha+\rho=1} \rightarrow \text{for opaque body.}$$

White body:- If all the incident radiation falling on the body are reflected called white body.

$$\boxed{\rho=1, \alpha=0, \tau=0} \rightarrow \text{for white body.}$$



Absorptivity:- The amount of heat absorbed by the body is called absorptivity.

Reflectivity:- The amount of heat reflected by the body is called Reflectivity.

Transmissivity:- The amount of heat transmitted by body is called transmissivity.

(679)

Stefan-Boltzmann law:- This law states that emissive power of a black body is directly proportional to the fourth power of its absolute temp.

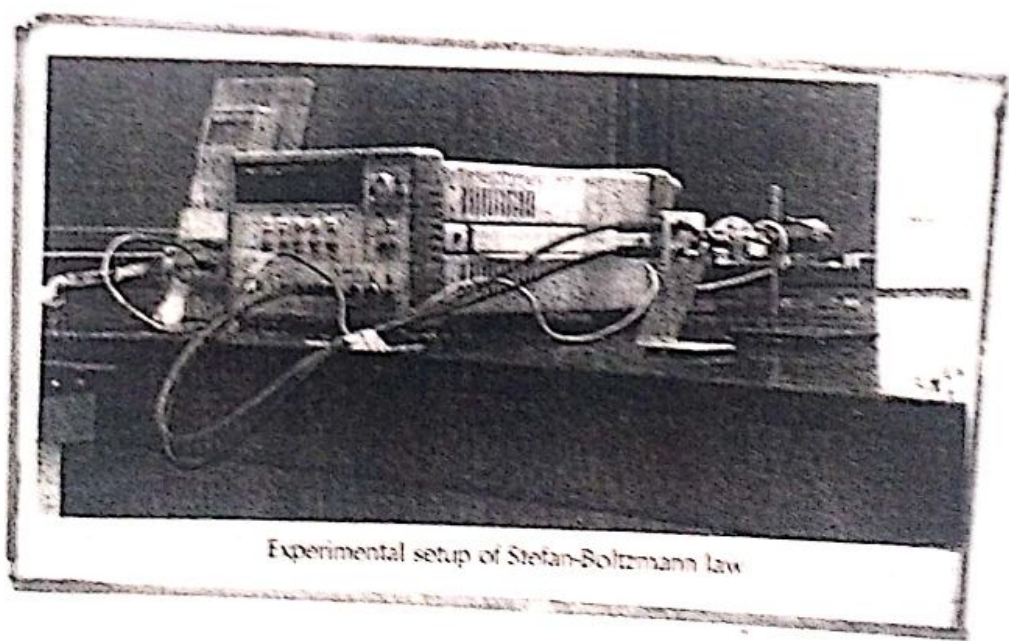
$$E_b = \sigma T^4$$

where,

E_b = emissive power of a black body.

σ = Stefan-boltz man constant

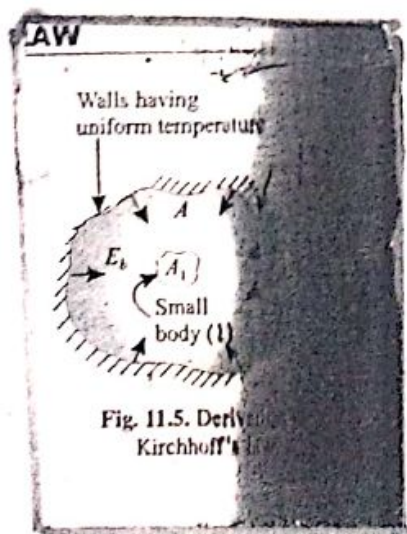
$$= 5.67 \times 10^{-8} \text{ W/m}^2 \text{K}^4$$



KIRCHOFF'S LAW :- The Law states that any at any temp, the ratio of total emissive power E to the total absorptivity α is a constant for all substances which are in thermal equilibrium with their environment.



Gustav Kirchhoff (1824-1887)



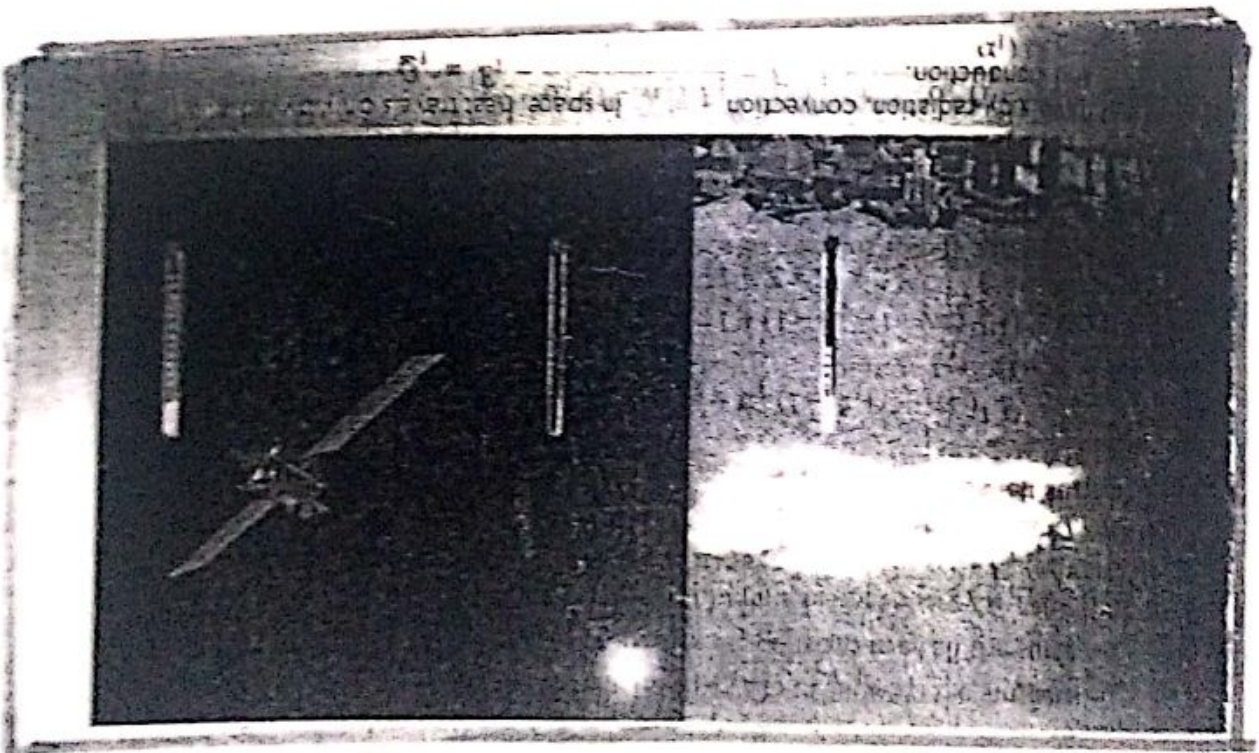
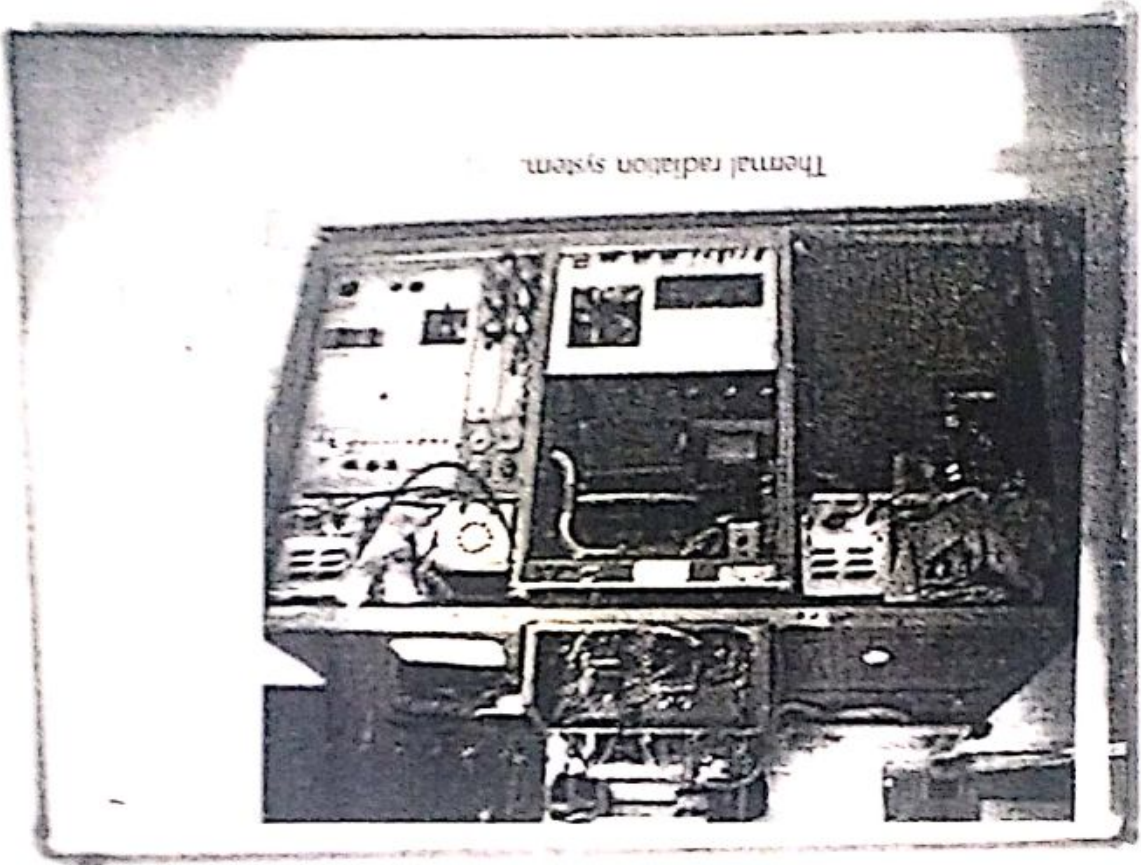


Table 12.1. Geometric (F_{1-2}) and Interchange (F_{1-2}) factors

No.	Configuration	Geometric factor (F_{1-2})	Interchange factor (F_{1-2})
	Infinite parallel planes	1	$\frac{1}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1}$
	Infinitely long concentric cylinders or concentric spheres	1	$\frac{1}{\frac{1}{\epsilon_1} + \frac{A_1}{A_2} \left(\frac{1}{\epsilon_2} - 1 \right)}$
	Body 1 (small) enclosed by body 2	1	ϵ_1
	Body 1 (large) enclosed by body 2	1	$\frac{1}{\frac{1}{\epsilon_1} + \frac{A_1}{A_2} \left(\frac{1}{\epsilon_2} - 1 \right)}$
	Two rectangles with common side at right angles to each other	1	$\epsilon_1 \epsilon_2$

Q. Calculate the following for an industrial furnace in the form of a black body & emitting radiation at 2500°C

- (i) monochromatic emissive power at $1.2\ \mu\text{m}$
- (ii) wavelength at which the emission is maximum.
- (iii) max. emissive power.
- (iv) total emissive power

Sol Given Data.

$$T = 2500 + 273$$
$$= 2773\ \text{K}$$

$$\lambda = 1.2\ \mu\text{m}$$

$$\varepsilon = 0.9$$

(i) According to Planck's law

$$(E_{\lambda})_b = \frac{C_1 \lambda^{-5}}{\exp\left(\frac{C_2}{\lambda T}\right) - 1}$$

$$C_1 = 3.742 \times 10^8\ \text{W}\cdot\mu\text{m}^4/\text{m}^2$$

$$= 0.3742 \times 10^{-15}\ \text{W}\cdot\text{m}^4/\text{m}^2$$

$$C_2 = 1.4388 \times 10^{-2}\ \text{m}\cdot\text{K}$$

$$(E_b)$$

$$= 0.3742 \times 10^{-15} \times (1.2 \times 10^{-6})^5$$

$$\frac{\exp\left(\frac{1.4388 \times 10^2}{1.2 \times 10^{-6} \times 2773}\right) - 1}$$

$$= 2.014 \times 10^{12} \text{ W/m}^2$$

(ii) According to Wien's Displacement Law

$$\lambda_{\max} = \frac{2898}{T}$$

$$= \frac{2898}{2773} = 1.045 \text{ } \mu\text{m}$$

$$(iii) (E_b)_{\max}$$

$$= 1.285 \times 10^{-5} \text{ W/m}^2 \text{ per meter length}$$

$$= 1.285 \times 10^{-5} \times (2773)^5$$

$$= 2.1 \times 10^{12} \text{ W/m}^2 \text{ per meter length}$$

(iv) Total emissive power

$$E_b = \sigma T^4$$

$$= 5.67 \times 10^{-8} (2773)^4$$

$$= 3.352 \times 10^6 \text{ W/m}^2$$

Q. The effective temp of a body having an area of 0.12 m^2 is 527°C . Calculate the following.

- (i) total rate of energy emission.
- (ii) intensity of normal radiation.

Sol Given Data

$$A = 0.12 \text{ m}^2$$

$$T = 527 + 273$$
$$= 800 \text{ K}$$

$$(i) E_b = \sigma A T^4 \text{ W}$$

$$= 5.67 \times 10^{-8} \times 0.12 \times (800)^4$$
$$= 2786.9 \text{ W}$$

$$(ii) I_{bn} = \frac{E_b}{\pi}$$

$$= \frac{\sigma T^4}{\pi} \Rightarrow \frac{5.67 \times \left(\frac{800}{100}\right)^4}{\pi}$$

$$= 7392.5 \text{ W/m}^2 \cdot \text{sr}$$

Q. Figure shows a cavity having surface temp as 900°C & emissivity as 0.6. Find the rate of emission from the cavity to surroundings.

707

Sol

$$Q = A_1 \epsilon_1 \sigma T_1^4 \left[\frac{1 - F_{1-1}}{1 - (1 - \epsilon_1) F_{1-1}} \right]$$

$A_1 =$ area of cavity.

$A_2 =$ " " opening of cavity

$$= \frac{\pi}{4} d^2 L$$

$$= \frac{\pi}{4} \times \left(\frac{5}{100} \right)^2$$

$$= 0.001963 \text{ m}^2$$

$$A_1 = A_f + A_{hs}$$

$A_f =$ Area of frustum

$A_{hs} =$ Area of half sphere.

$$A_f = \pi (\delta_1 + \delta_2) \sqrt{(\delta_2 - \delta_1)^2 + h^2}$$

$$r_1 = 2.5 \text{ cm}$$

$$r_2 = 5 \text{ cm}$$

$$h = 4 \text{ cm}$$

$$A_f = \pi (2.5 + 5) \sqrt{(5 - 2.5)^2 + 4^2}$$
$$= 0.01111 \text{ m}^2$$

$$A_{hs} = \frac{1}{2} \times 4\pi r^2$$
$$= 2\pi r^2$$
$$= 0.0157 \text{ m}^2$$

$$A_1 = 0.01111 + 0.0157$$
$$= 0.0268 \text{ m}^2$$

$$F_{1-1} = 1 - \frac{A_2}{A_1} = 1 - \frac{0.001963}{0.0268}$$
$$= 0.926$$

$$Q = 0.0268 \times 0.6 \times 5.67 \left(\frac{900 + 273}{100} \right)^4 \left(\frac{1 - 0.926}{1 - (1 - 0.6) \times 0.926} \right)$$
$$= 202.87 \text{ W}$$

④ The filament of a 75 W light bulb may be considered a black body radiating into a black enclosure at 70°C . The filament dia 0.10 mm & $L = 5 \text{ cm}$.

$$\text{Sol } Q = 75 \text{ W}$$

$$= 75 \text{ J/s}$$

$$T_2 = 30 + 273$$

$$= 303 \text{ K}$$

$$d = 0.01 \text{ m}$$

$$l = 5 \text{ cm}$$

$$Q = \sigma \epsilon A (T_1^4 - T_2^4)$$

$$75 = 5.67 \times 10^{-8} \times l \times (\pi d l) \times (T_1^4 - T_2^4)$$

$$75 = 5.67 \times 10^{-8} \times (\pi \times 0.01 \times 10^3 \times 5 \times 10^{-2}) (T_1^4 - 303^4)$$

$$T_1^4 = \frac{75}{5.67 \times 10^{-8}} + (303)^4$$

$$T_1^4 = 8.42 \times 10^3 + (303)^4$$

$$T_1 = \sqrt[4]{8.42 \times 10^3 + 303^4}$$

$$T_1 = 275.6^\circ \text{C}$$

5. Two parallel rectangular surfaces $1 \text{ m} \times 2 \text{ m}$ are opposite to each other at a distance of 4 m . The surfaces are black & at 100°C & 200°C . Calculate the heat exchange by radiation b/w 2 surfaces.

$$\text{Sol} \quad Q_{12} = A_1 F_{1-2} \sigma (T_1^4 - T_2^4)$$

$$\epsilon_1 = \epsilon_2 = 1$$

$$\frac{X}{L} = \frac{2}{4} = 0.5 \text{ (from tables)}$$

$$\frac{Y}{L} = \frac{1}{4} = 0.25$$

$$F_{1-2} = 0.043$$

$$Q_{12} = (2 \times 1) \times 0.043 \times 5.67$$

$$= 149.5 \text{ Watts}$$

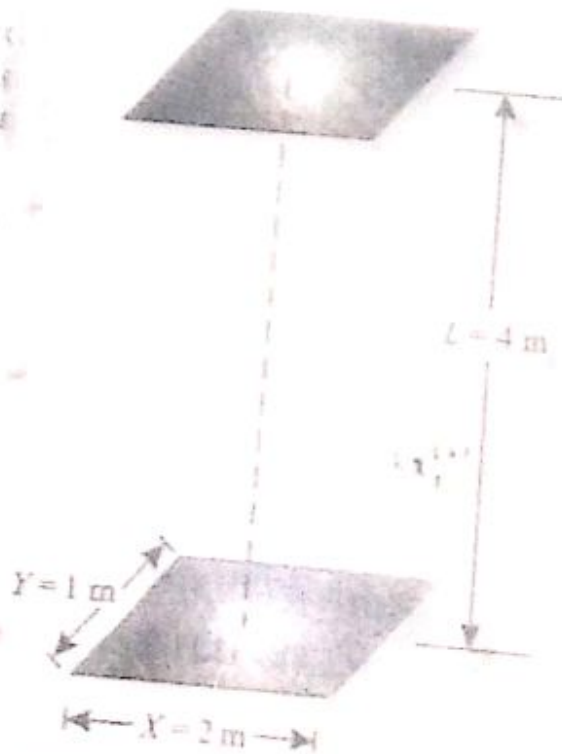


FIG. 12.20